



# Tests of Lepton Flavour Universality at LHCb

*First Angular Analysis of  $B^0 \rightarrow K^{*0} e^+ e^-$  decay at the central  $q^2$*

[LHCb-PAPER-2024-022, Preliminary]

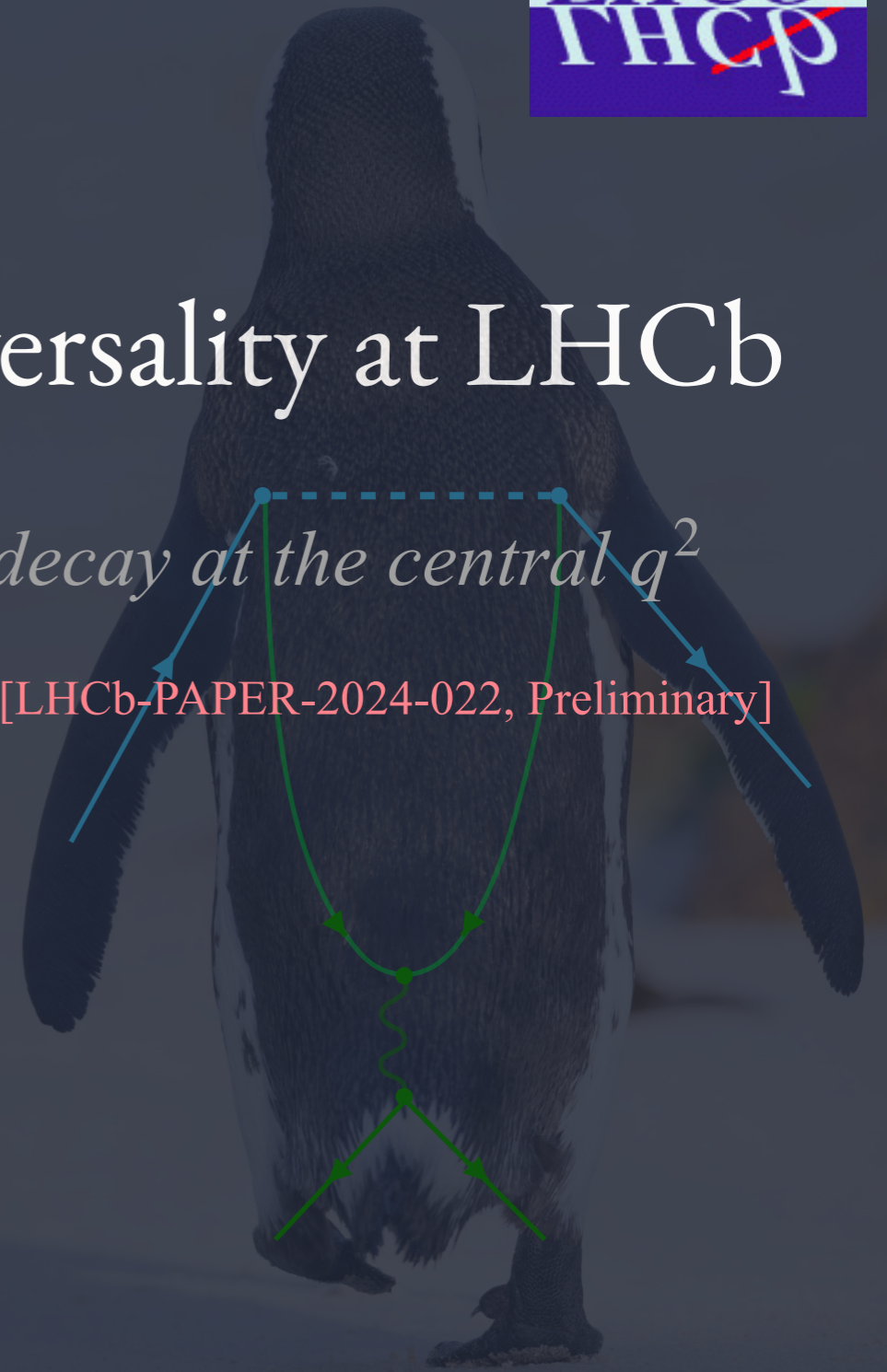
Rafael Silva Coutinho

Syracuse University

On behalf of the LHCb Collaboration

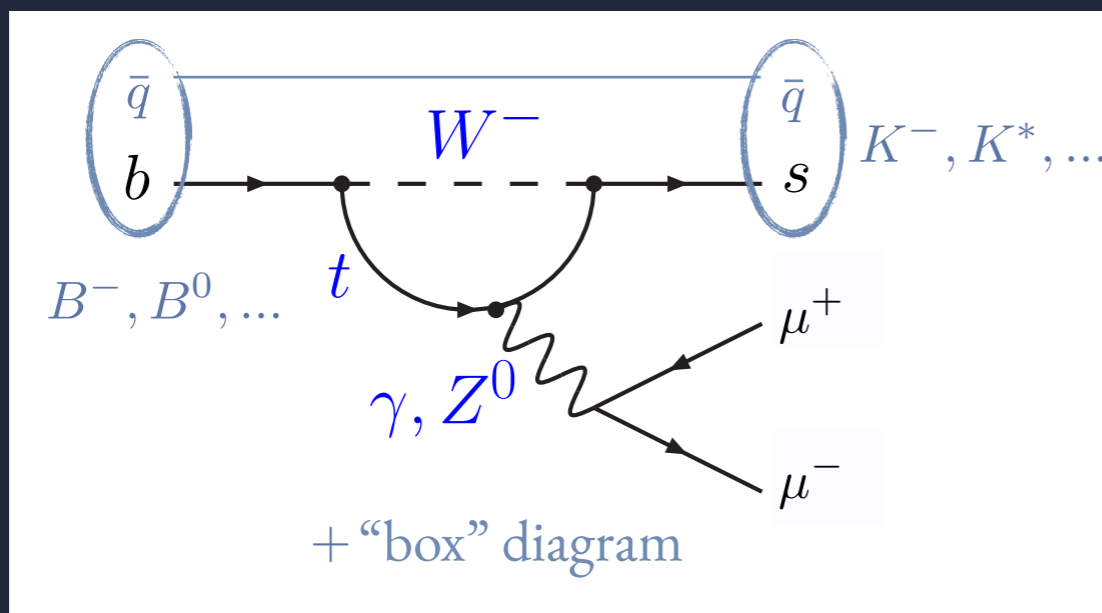
42<sup>nd</sup> International Conference on High Energy Physics

Prague, July 19<sup>th</sup>, 2024



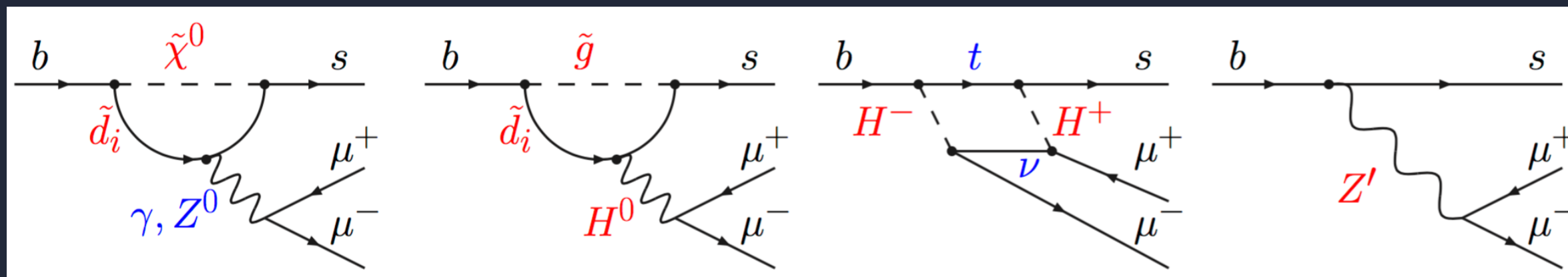
# RARE DECAYS AS A PROBE OF NEW PHYSICS

FCNC: UNIQUE GLIMPSE TO HIGHER SCALE



[E.G. ENHANCEMENT/SUPPRESSION OF  
 DECAY RATE, ANGULAR DISTRIBUTIONS  
 AND NEW SOURCES OF CP]

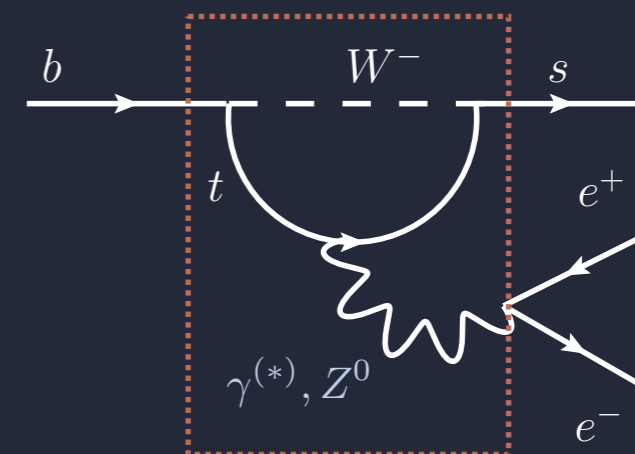
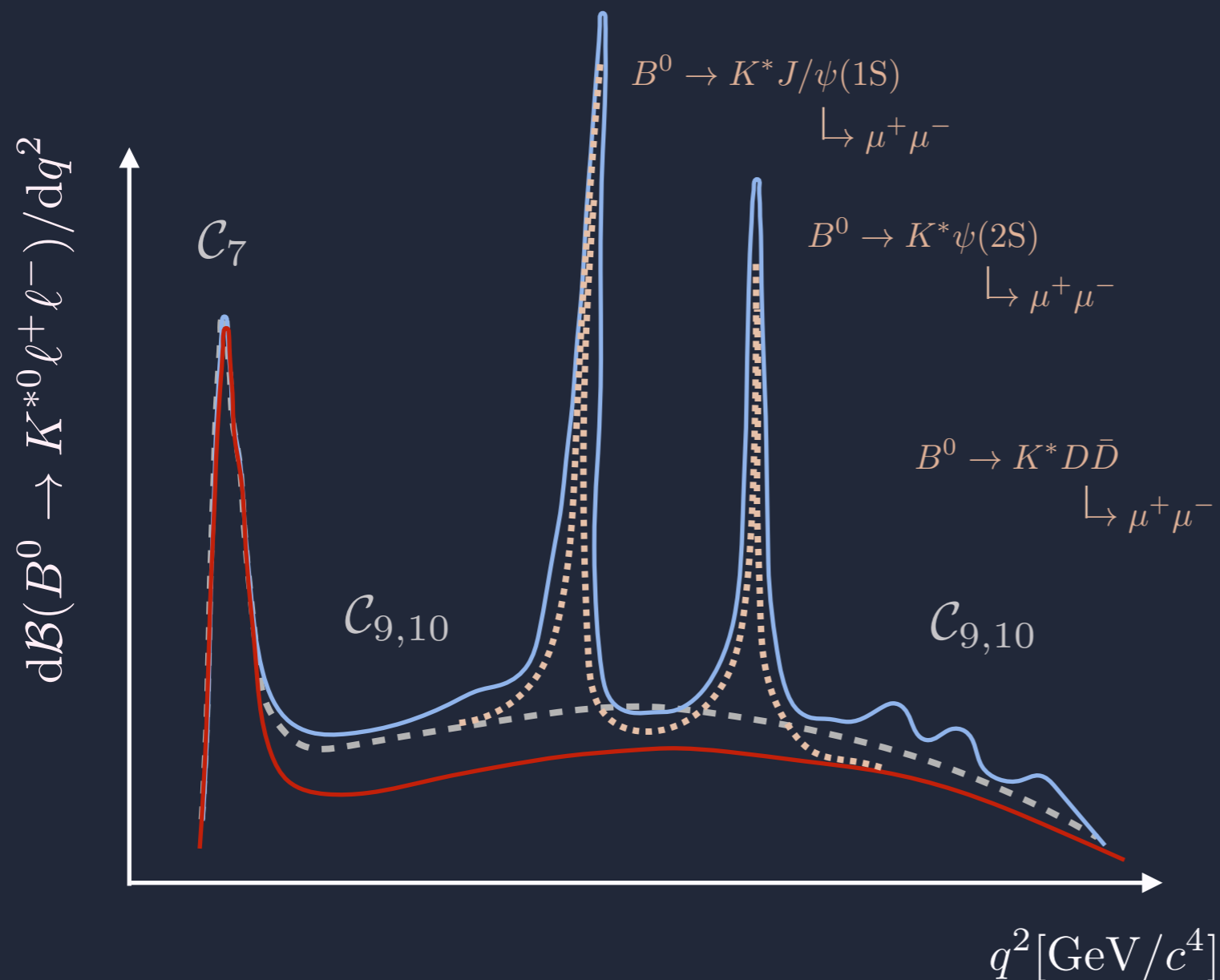
NEW PARTICLES CAN CONTRIBUTE AT LOOP AND/OR TREE LEVEL



# THE $B^0 \rightarrow K^{*0} \ell^+ \ell^-$ DECAY

FCNC EFFECTIVE HAMILTONIAN DESCRIBED AS OPE

FLAVOUR CHANNEL NEUTRAL CURRENT DESCRIBED IN AN EFFECTIVE FIELD THEORY



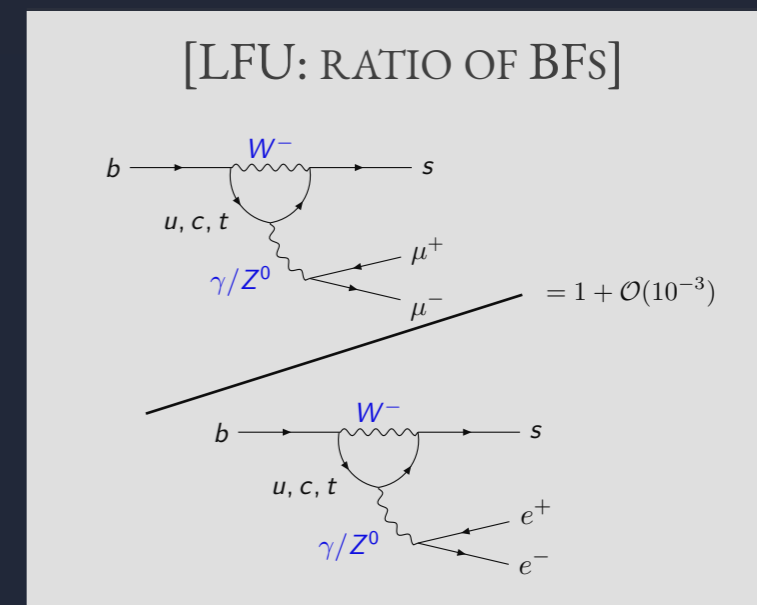
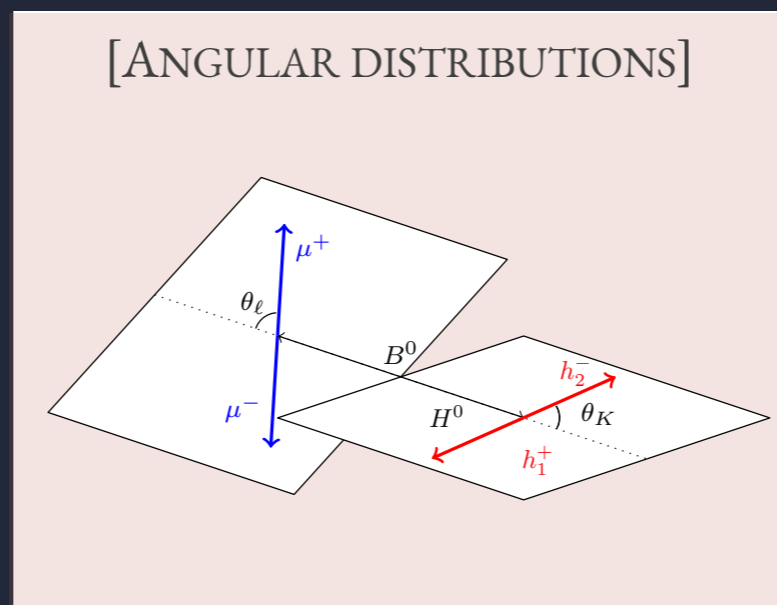
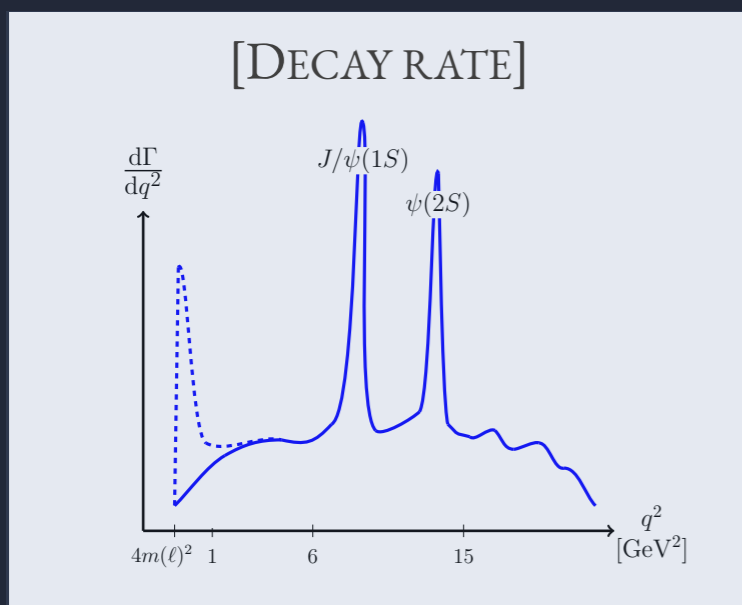
$C_7, C_{9,10}$

$$C_i = C_i^{\text{SM}} + C_i^{\text{NP}} + C_i^{\text{had}}$$

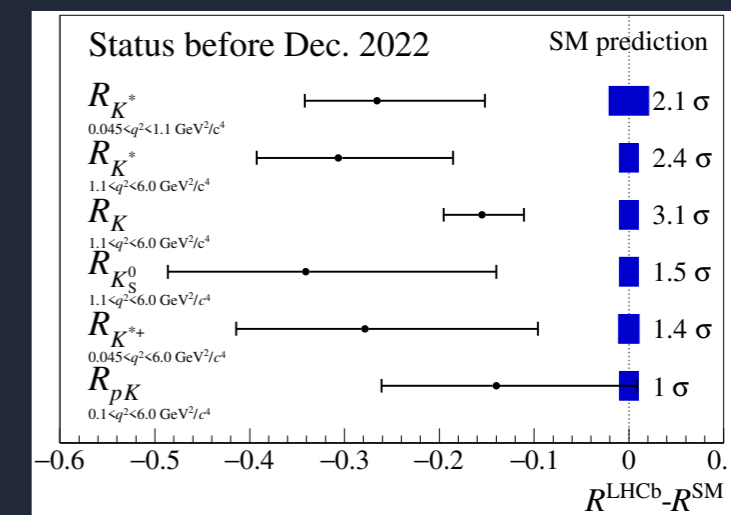
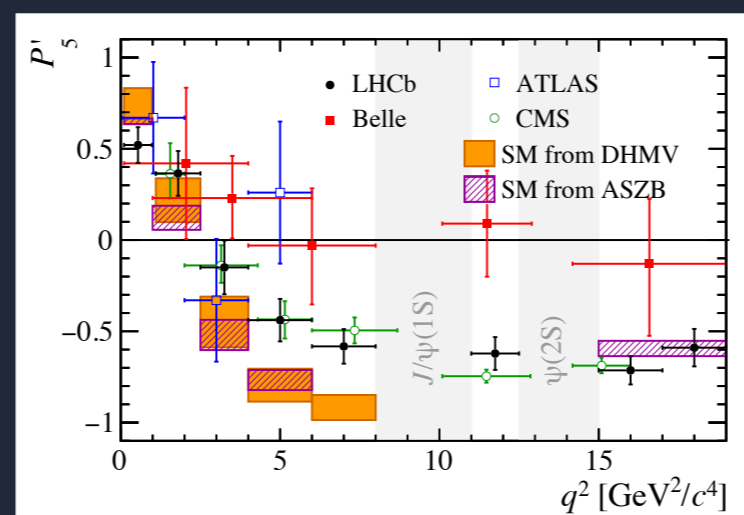
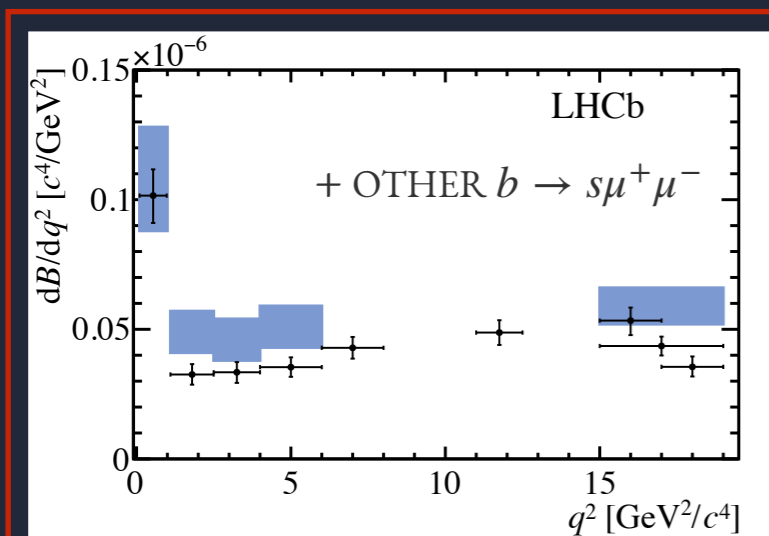
# FLAVOUR ANOMALIES IN $b \rightarrow s\ell^+\ell^-$

HIGH THEORETICAL UNCERTAINTY

LOW THEORETICAL UNCERTAINTY



CONSISTENT ANOMALOUS PATTERN

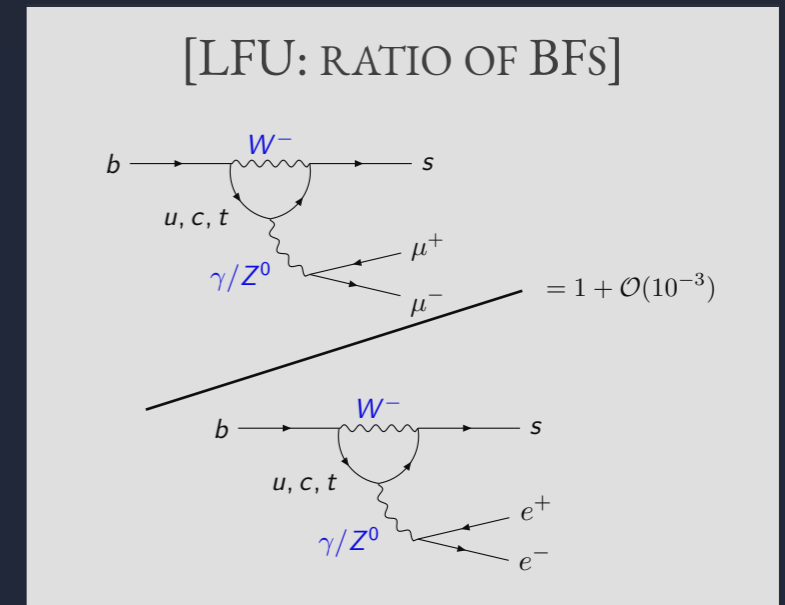
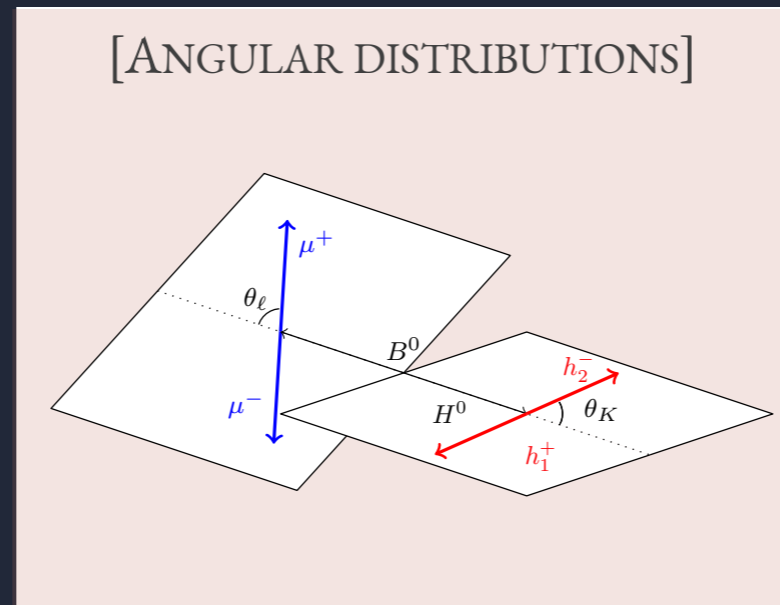
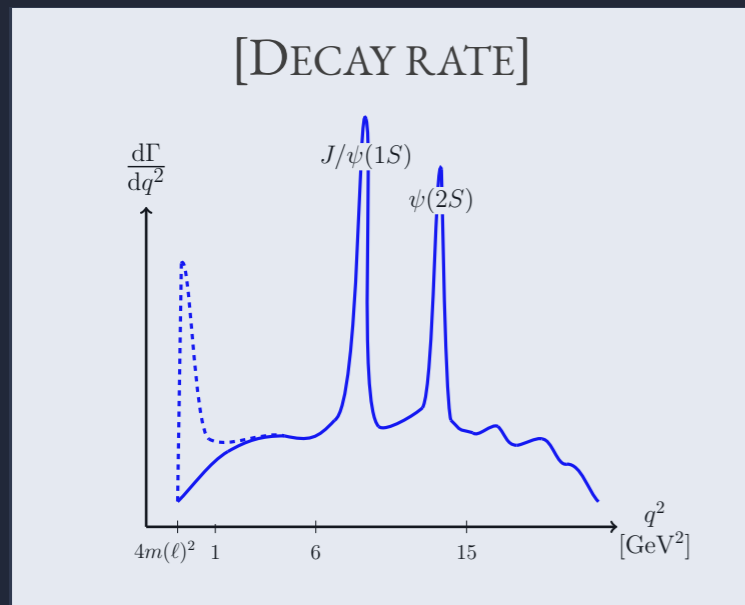




# FLAVOUR ANOMALIES IN $b \rightarrow s\ell^+\ell^-$

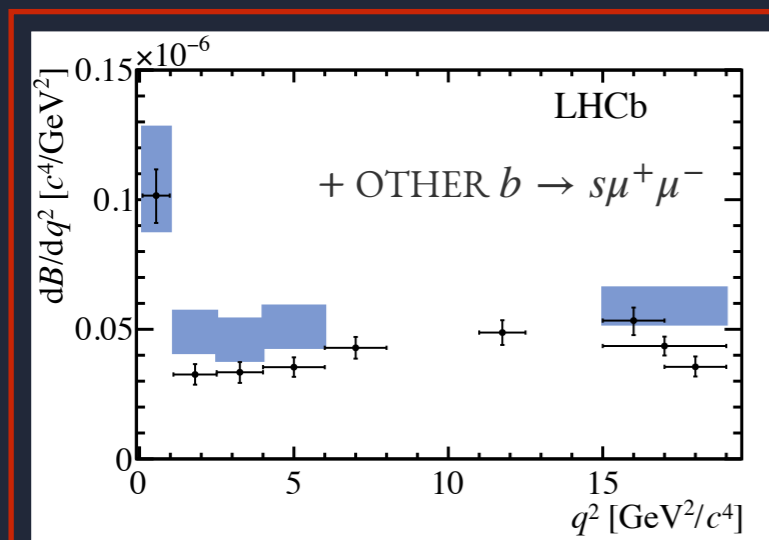
HIGH THEORETICAL UNCERTAINTY

LOW THEORETICAL UNCERTAINTY

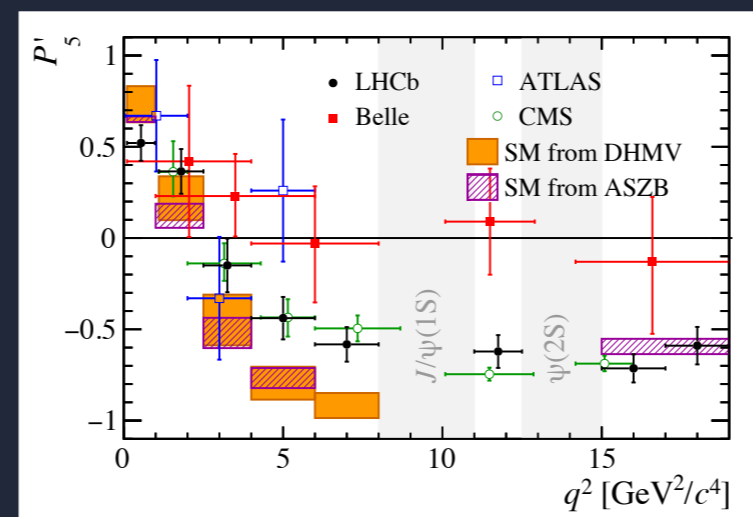


CONSISTENT ANOMALOUS PATTERN

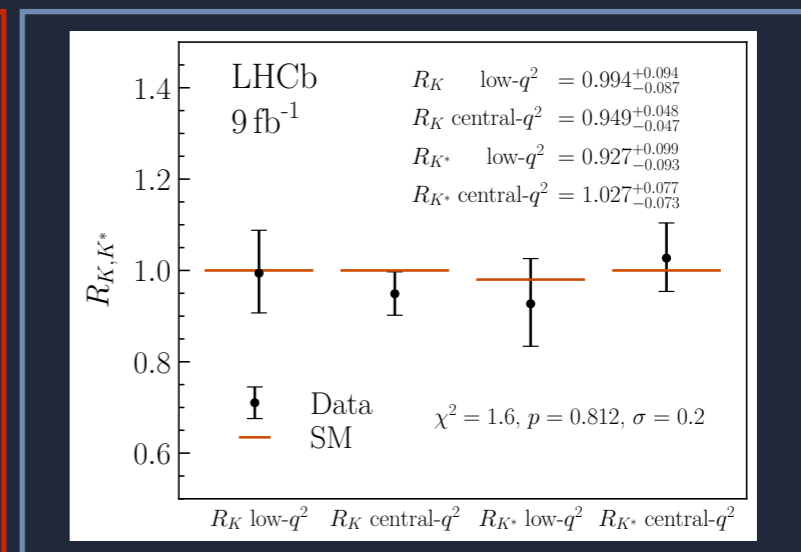
LFU CONSISTENT WITH SM!



[LHCb, JHEP 11 (2016) 047]



[LHCb, PRL 125 (2020) 011802  
Belle, PRL 118 (2017) 11, 111801  
ATLAS, JHEP 10 (2018) 047  
CMS, PLB 781 (2018) 517]

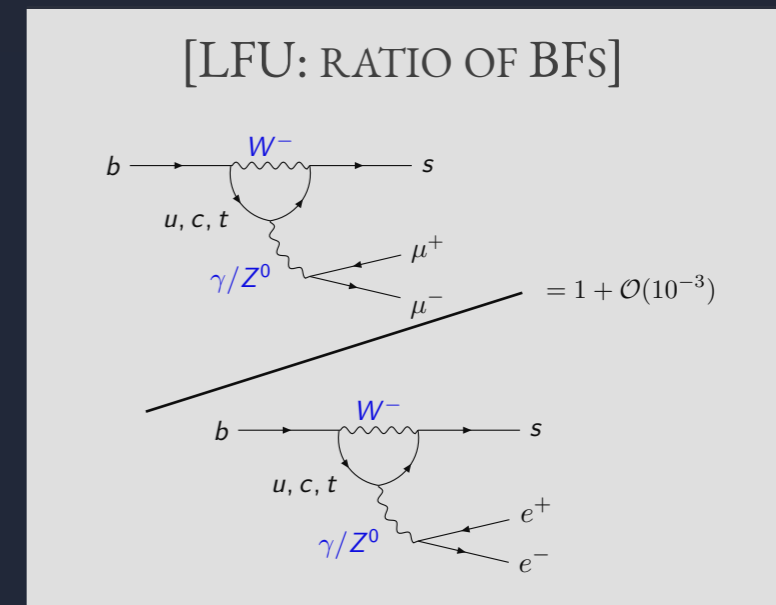
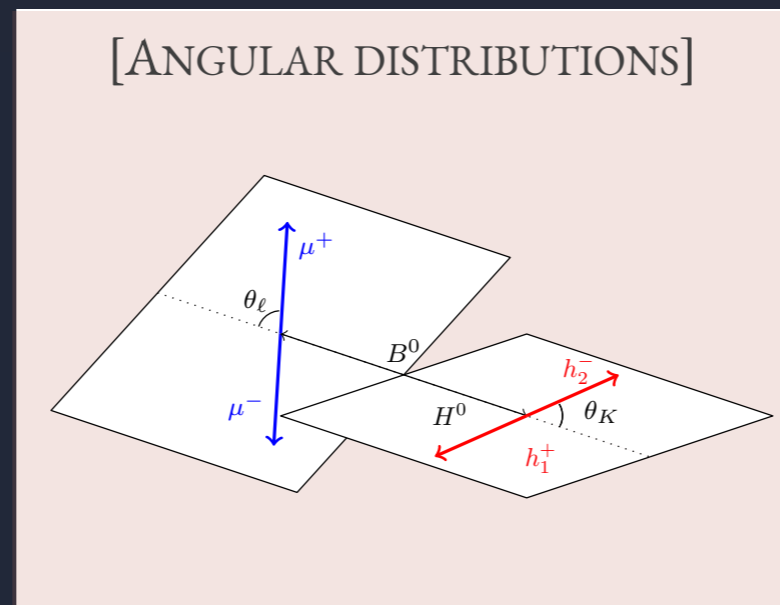
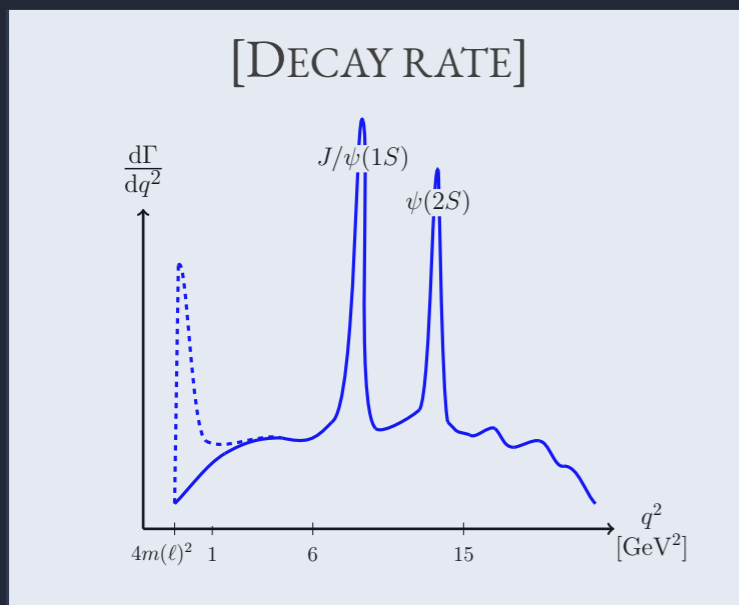


[LHCb, PRL 131 (2023) 051803, PRD 108 (2023) 032002]

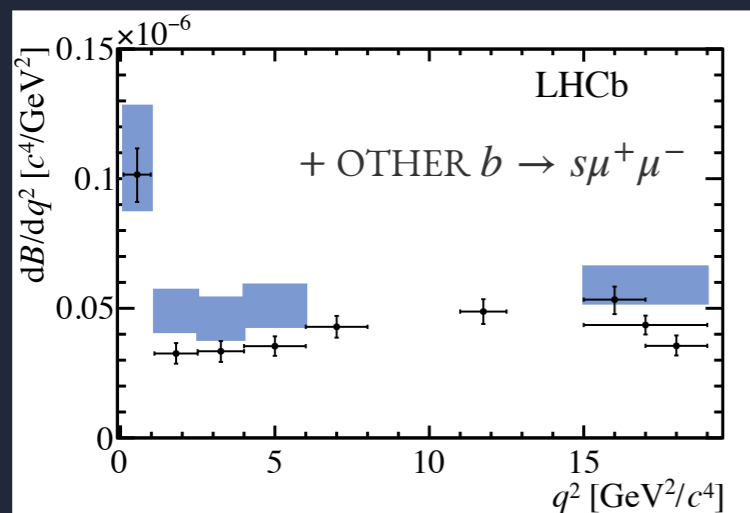
# FLAVOUR ANOMALIES IN $b \rightarrow s\ell^+\ell^-$

HIGH THEORETICAL UNCERTAINTY

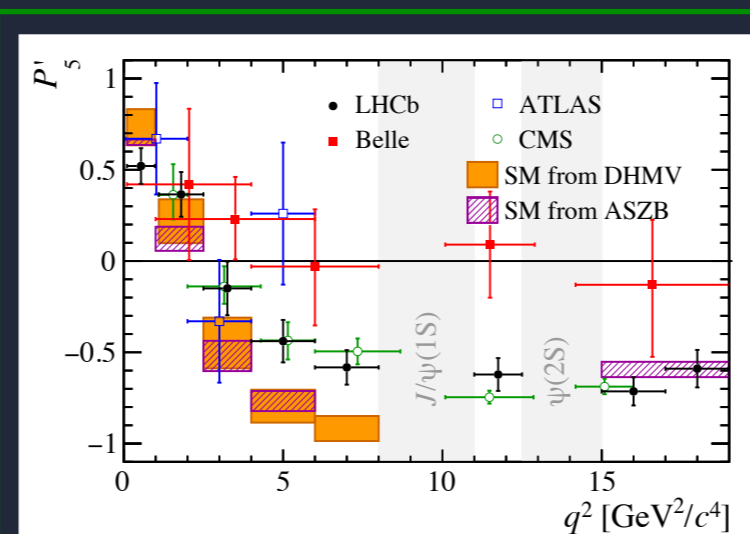
LOW THEORETICAL UNCERTAINTY



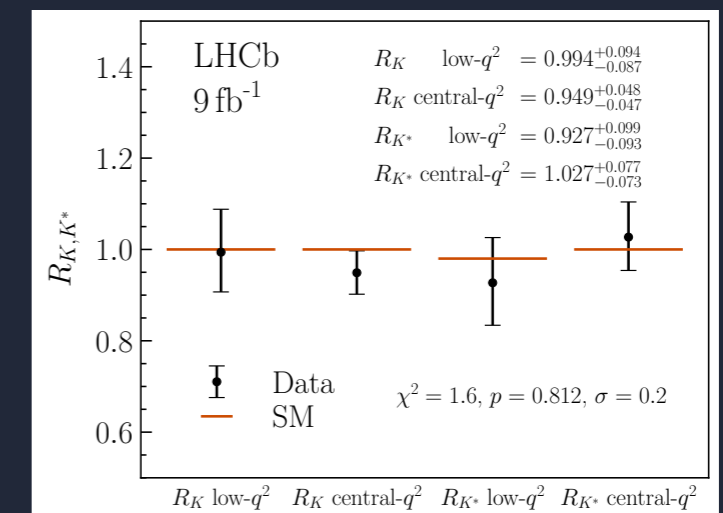
WHAT ABOUT LFU TESTS IN ANGULAR DISTRIBUTIONS?



[LHCb, JHEP 11 (2016) 047]



[LHCb, PRL 125 (2020) 011802  
Belle, PRL 118 (2017) 11, 111801  
ATLAS, JHEP 10 (2018) 047  
CMS, PLB 781 (2018) 517]




[LHCb, PRL 131 (2023) 051803, PRD 108 (2023) 032002]

# ANALYSIS STRATEGY


[LHCb-PAPER-2024-022, Preliminary]

FIRST ANGULAR ANALYSIS OF  $B^0 \rightarrow K^{*0}e^+e^-$  DECAYS AT THE CENTRAL  $q^2$  REGION

- FULL RUN 1 + 2  STATISTICS ( $9 \text{ fb}^{-1}$ )
  - ▶ SIMULTANEOUS FIT TO [2011-2012], [2015-2016] AND [2017-2018] DATASETS
- 4D UNBINNED WEIGHTED FIT TO THE MASS AND ANGULAR DISTRIBUTIONS

$$\text{PDF}(\vec{\Omega}, m | \vec{\Theta}, \vec{\lambda}) = f_{sig} \text{pdf}_{sig}(\vec{\Omega}, m | \vec{\Theta}, \vec{\lambda}) + \sum_i^{n-1} f_{bkg,i} \text{pdf}_{bkg,i}(\vec{\Omega}, m | \vec{\lambda}_{bkg,i}) + (1 - f_{sig} - \sum_i^{n-1} f_{bkg,i}) \text{pdf}_{bkg,n}(\vec{\Omega}, m | \vec{\lambda}_{bkg,n})$$

WITH LIKELIHOOD AS  $-\sum_{events,e} \frac{1}{\epsilon_e(\vec{\Omega}, q^2)} \cdot \ln \text{PDF}(\vec{\Omega}, m | \vec{\Theta}, \vec{\lambda})$  MASS AND ANGULAR DISTRIBUTIONS ARE ASSUMED TO FACTORISE

- SELECTION AND CORRECTIONS FOLLOW CLOSELY  $R_{K^*}$  ANALYSIS [PRL 131 (2023) 051803, PRD 108 (2023) 032002]
- DETERMINE CP-AVERAGED  $S_i$  AND CORRESPONDING OPTIMISED  $P_i^{(\cdot)}$  OBSERVABLES
- LFU OBSERVABLES  $Q_i$  ARE DERIVED BY COMPARING THE RESULTS AGAINST PREVIOUSLY PUBLISHED  MUON ANALYSIS

$$Q_i = P_i^{(\mu)} - P_i^{(e)}$$

[JHEP 10 (2016) 075]

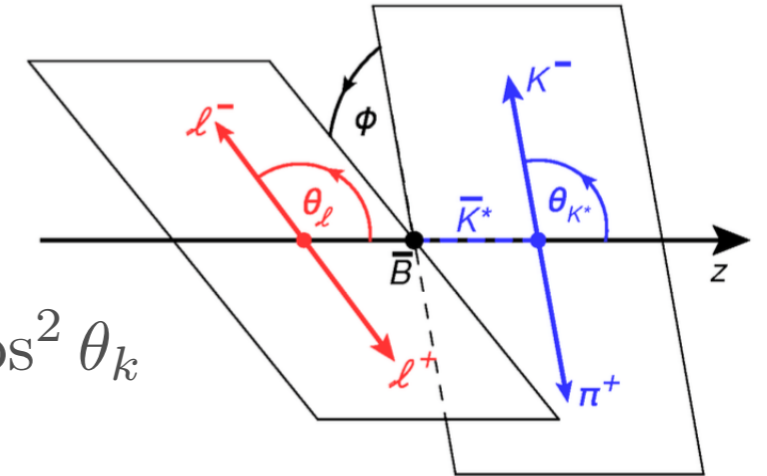
# THE RARE DECAY $B^0 \rightarrow K^{*0}[K^+\pi^-]e^+e^-$

DECAY FULLY DESCRIBED BY THREE HELICITY ANGLES

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_k + F_L \cos^2 \theta_k \right. \\ \left. + \frac{1}{4}(1 - F_L) \sin^2 \theta_k \cos 2\theta_l \right. \\ \left. - F_L \cos^2 \theta_k \cos 2\theta_l + S_3 \sin^2 \theta_k \sin^2 \theta_l \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_k \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_k \sin \theta_l \cos \phi \right. \\ \left. + \frac{4}{3} A_{FB} \sin^2 \theta_k \cos \theta_l + S_7 \sin 2\theta_k \sin \theta_l \sin \phi \right. \\ \left. + S_8 \sin 2\theta_k \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_k \sin^2 \theta_l \sin 2\phi \right]$$

Fraction of longitudinal  
polarisation of the  $K^*$

Forward-backward asymmetry  
of the di-lepton system



$F_L, A_{FB}$  AND  $S_i$  ARE COMBINATIONS OF  $K^{*0}$  SPIN AMPLITUDES SENSITIVE TO  $C_{7,9,10}^{(0)}$  AND FORM FACTORS

PERFORM RATIOS OF OBSERVABLES (E.G.  $P'_5$ ) WHERE FORM FACTORS CANCEL AT LEADING ORDER

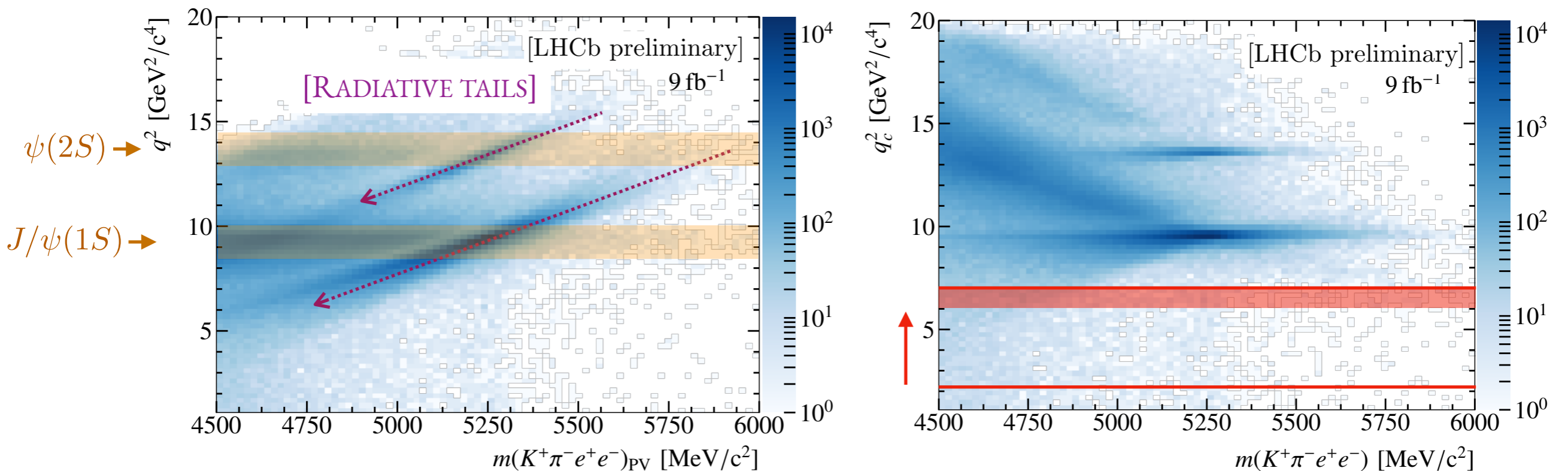
$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}} \quad [\text{JHEP 1204 (2012) 104}]$$

\*S-WAVE CONTRIBUTION IS CONSIDERED IN THE SYSTEMATICS

# DATA SELECTION

IMPROVED STRATEGY TO CONTROL SIGNAL RESOLUTION IN ELECTRONS:

$q^2$  DEFINED WITH  $B^0$  PRIMARY VERTEX AND  $B^0$  MASS CONSTRAINT, ALLOWING FOR THE EXTENSION OF THE ANALYSIS RANGE UP TO  $7.0 \text{ GeV}^2/c^4$  AND REDUCED BIN MIGRATION



ANALYSIS PERFORMED IN TWO  $q^2$  REGIMES:  $[1.1, 6.0]$  AND  $[1.1, 7.0] \text{ GeV}^2/c^4$



# ACCEPTANCE EFFECTS

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ANGULAR AND  $q^2$  DISTRIBUTIONS ARE DISTORTED BY THE EFFICIENCY OF THE SELECTION AND RECONSTRUCTION, AND RESOLUTION EFFECTS

EFFICIENCY PARAMETRISED IN **4D** USING LEGENDRE POLYNOMIAL FOR ALL VARIABLES EXCEPT PHI (FOURIER):

$$\epsilon(\cos \theta_\ell, \cos \theta_K, \phi, q_c^2) = \sum_{k,l,m,n} c_{k,l,m,n} L_k(\cos \theta_K) L_l(\cos \theta_\ell) F_m(\phi) L_n(q_c^2)$$

COEFFICIENTS ARE OBTAINED FROM SIMULATION USING METHOD OF MOMENTS:

$$c_{k,l,m,n} = \frac{1}{N'} \sum_{i=1}^N w_i \left[ \left( \frac{2k+1}{2} \right) \left( \frac{2l+1}{2} \right) \left( \frac{2m+1}{2} \right) \left( \frac{2n+1}{2} \right) \right]$$

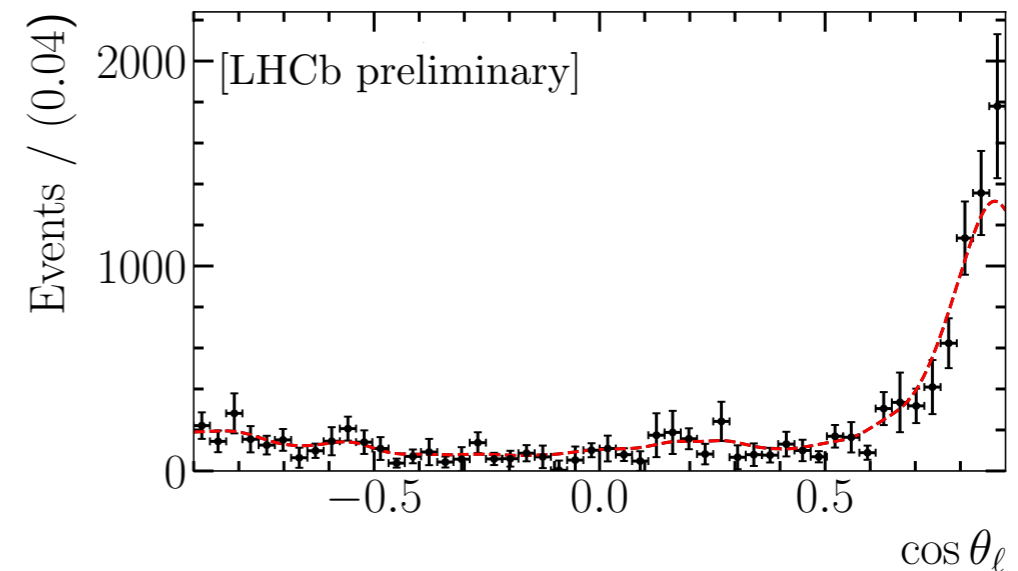
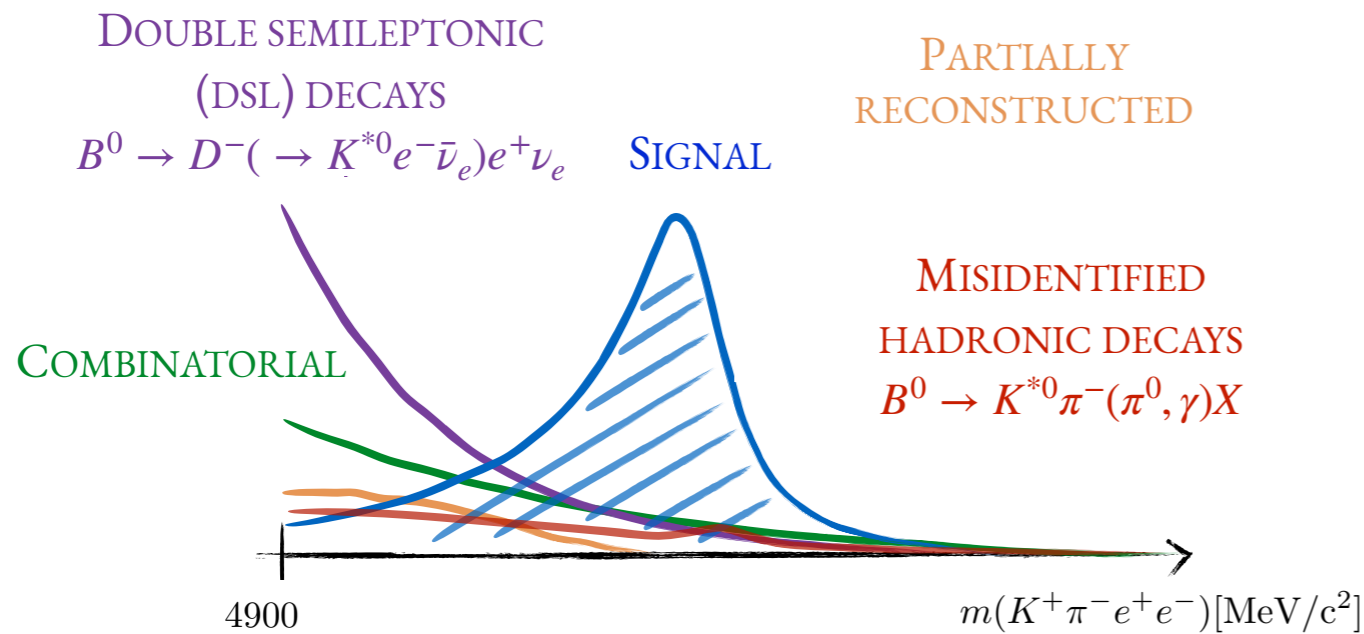
WEIGHTS ACCOUNT FOR DATA SIMULATION DIFFERENCES

# SIGNAL/BACKGROUND SEPARATION

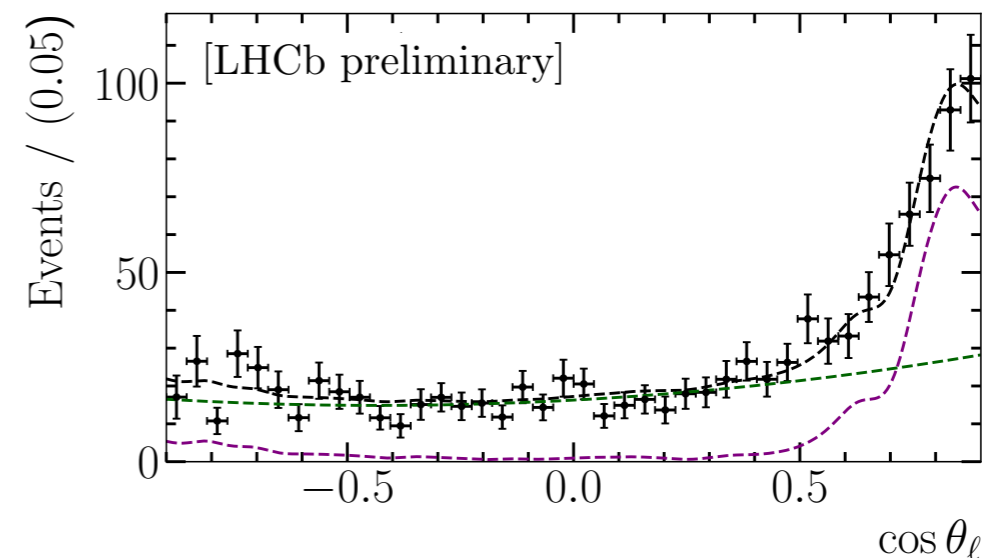
CONTROL OVER BACKGROUND CONTRIBUTIONS REQUIRES KNOWLEDGE OF THE MASS AND ANGULAR STRUCTURE

PASS-FAIL METHOD (INVERTED PID)

[PRL 131 (2023) 051803, PRD 108 (2023) 032002]



$B^0 \rightarrow K^{*0} e^+ \mu^-$  (LFV) DATA



DATA-DRIVEN STRATEGY USED TO OBTAIN AN EFFECTIVE LINESHAPE USING CONTROL SAMPLES

# SYSTEMATIC UNCERTAINTIES

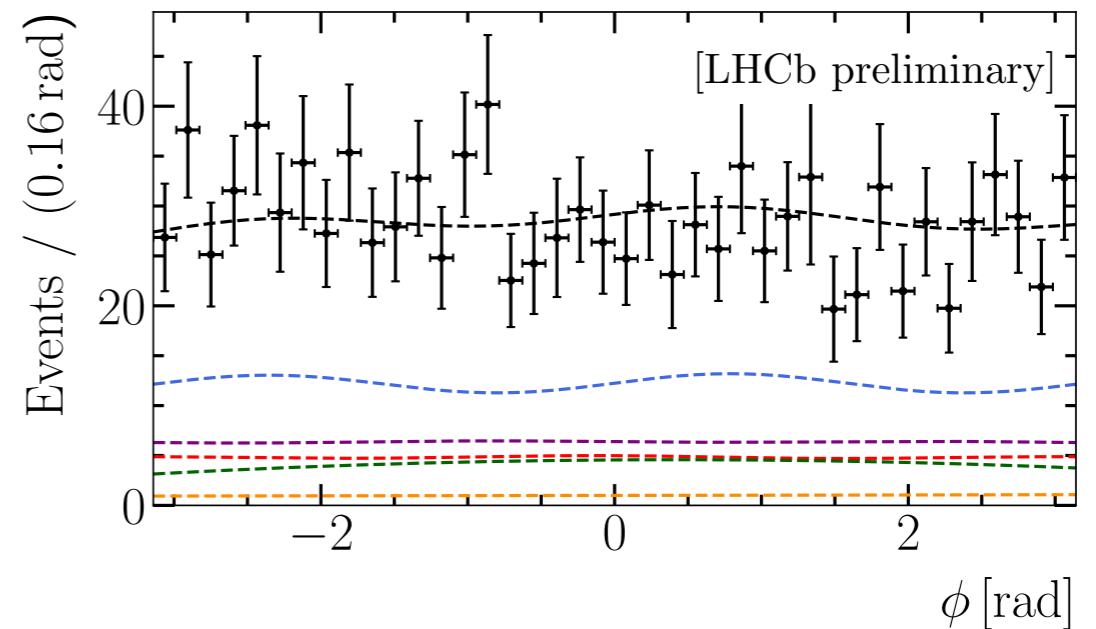
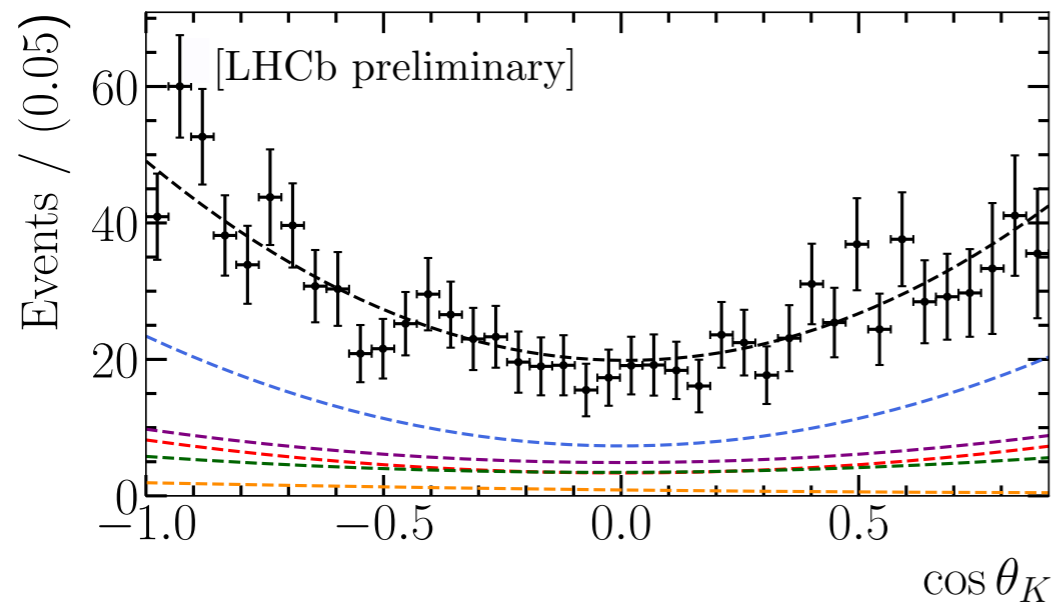
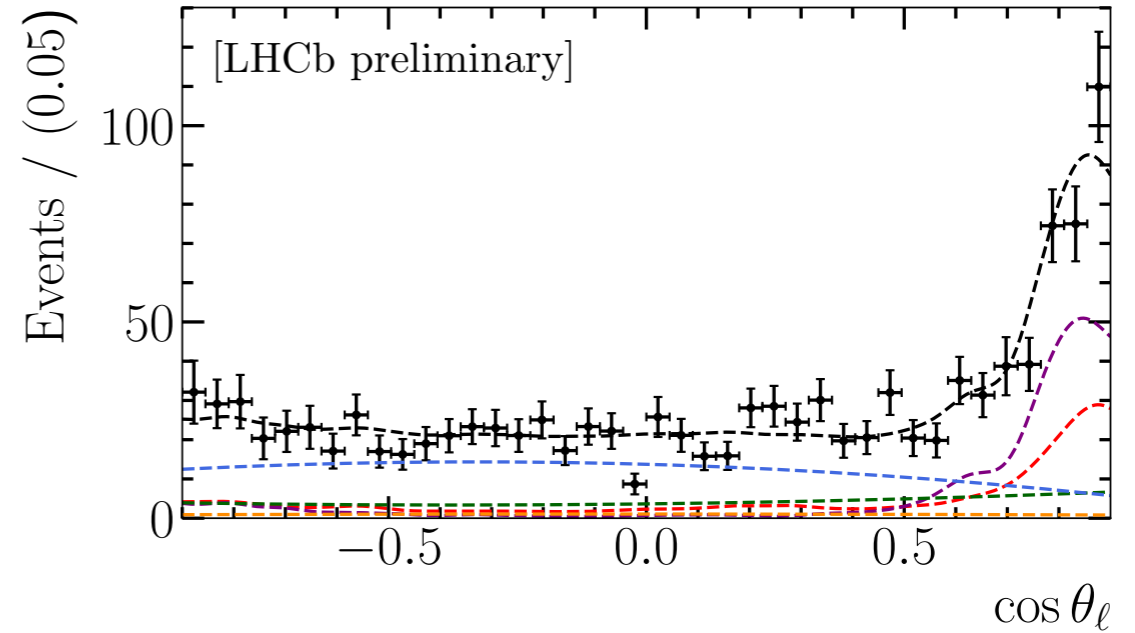
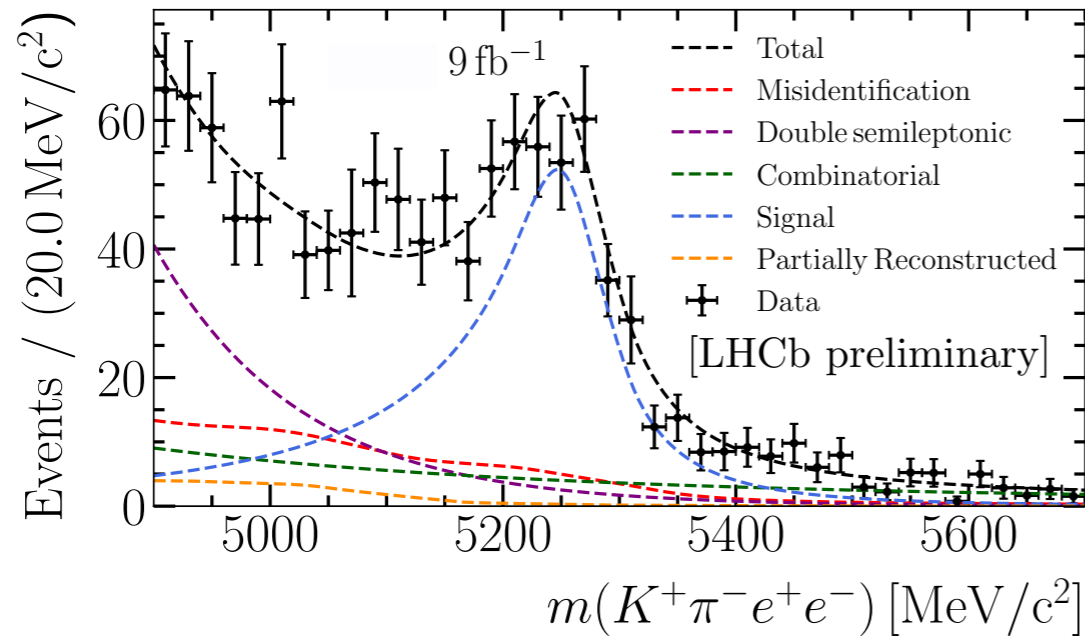
LARGEST UNCERTAINTIES ARE MOSTLY ASSOCIATED TO ASSUMPTIONS ON THE EFFECTIVE BACKGROUND MODELLING

	$F_L$	$S_3$	$S_4$	$S_5$	$A_{FB}$	$S_7$	$S_8$	$S_9$
DSL and comb.	0.687	0.372	0.297	0.321	0.449	0.177	0.668	0.294
Part. reco.	0.091	0.039	0.039	0.049	0.051	0.021	0.034	0.037
Had. misid.	0.376	0.254	0.107	0.178	0.155	0.336	0.129	0.141
Effective acceptance	0.399	0.249	0.419	0.410	0.331	0.508	0.393	0.214
Signal mass modelling	0.254	0.057	0.071	0.111	0.122	0.044	0.045	0.062
Residual backgrounds	0.179	0.039	0.045	0.062	0.137	0.032	0.032	0.047
S-wave component	0.351	0.050	0.129	0.084	0.105	0.159	0.008	0.103
$B^+$ veto	0.499	0.133	0.152	0.179	0.242	0.159	0.154	0.117
Fit bias	0.007	0.008	0.030	0.038	0.042	0.007	0.019	0.031
Total*	1.118	0.540	0.570	0.601	0.665	0.676	0.804	0.430

\*VALUES ARE GIVEN RELATIVE TO THE STATISTICAL UNCERTAINTIES

- $F_L$ ,  $A_{FB}$  AND  $S_8$  ARE PARTICULARLY AFFECTED BY CHOICES ON THE DOUBLE SEMILEPTONIC AND COMBINATORIAL PARAMETRISATION
- SIZEABLE IMPACT OF THE ACCEPTANCE MODELLING (DATA/SIMULATION CORRECTIONS)

# DATA FIT PROJECTIONS

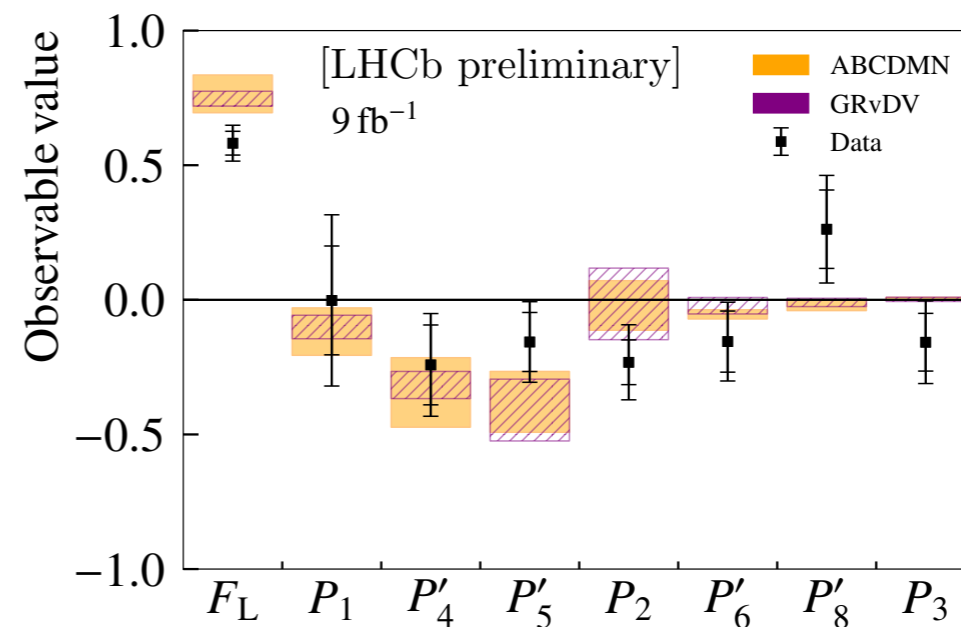
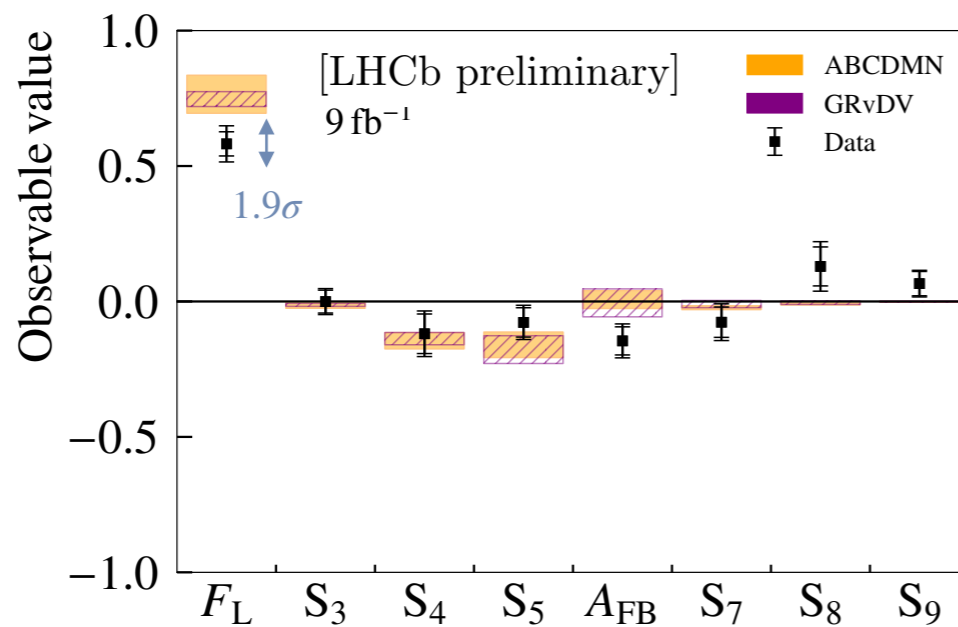


# DATA FIT RESULTS SUMMARY

$$1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$$

$F_L$	$0.582 \pm 0.045 \pm 0.050$		
$S_3$	$-0.000 \pm 0.042 \pm 0.023$	$P_1$	$-0.002 \pm 0.202 \pm 0.246$
$S_4$	$-0.119 \pm 0.073 \pm 0.042$	$P'_4$	$-0.242 \pm 0.148 \pm 0.120$
$S_5$	$-0.077 \pm 0.054 \pm 0.033$	$P'_5$	$-0.157 \pm 0.110 \pm 0.102$
$A_{\text{FB}}$	$-0.146 \pm 0.052 \pm 0.035$	$P_2$	$-0.232 \pm 0.083 \pm 0.112$
$S_7$	$-0.077 \pm 0.056 \pm 0.038$	$P'_6$	$-0.155 \pm 0.114 \pm 0.092$
$S_8$	$0.129 \pm 0.072 \pm 0.056$	$P'_8$	$0.262 \pm 0.146 \pm 0.137$
$S_9$	$0.066 \pm 0.045 \pm 0.020$	$P_3$	$-0.157 \pm 0.107 \pm 0.110$

OVERALL GOOD AGREEMENT  
WITH SM PREDICTIONS



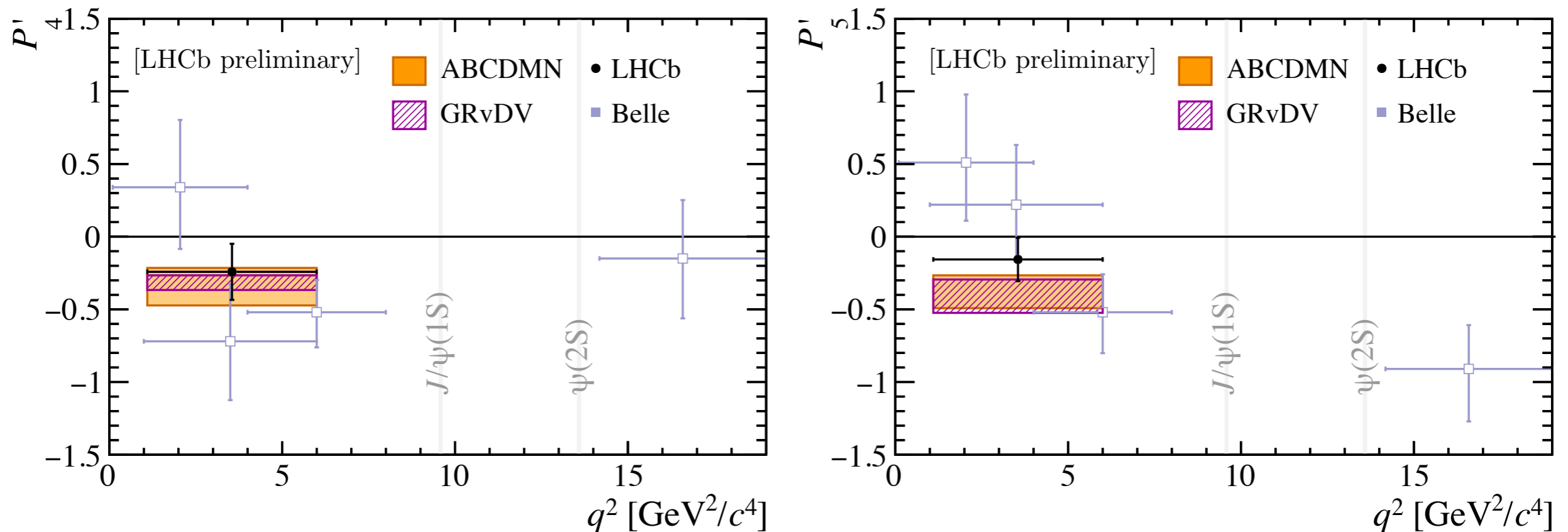
[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]



# OPTIMISED ANGULAR OBSERVABLES

SIMILAR PATTERN OBSERVED IN THE  $P_i^{(\prime)}$  BASIS



**MOST PRECISE DETERMINATION OF ANGULAR OBSERVABLES**

[Belle Collaboration, PRL 118 (2017) 111801]

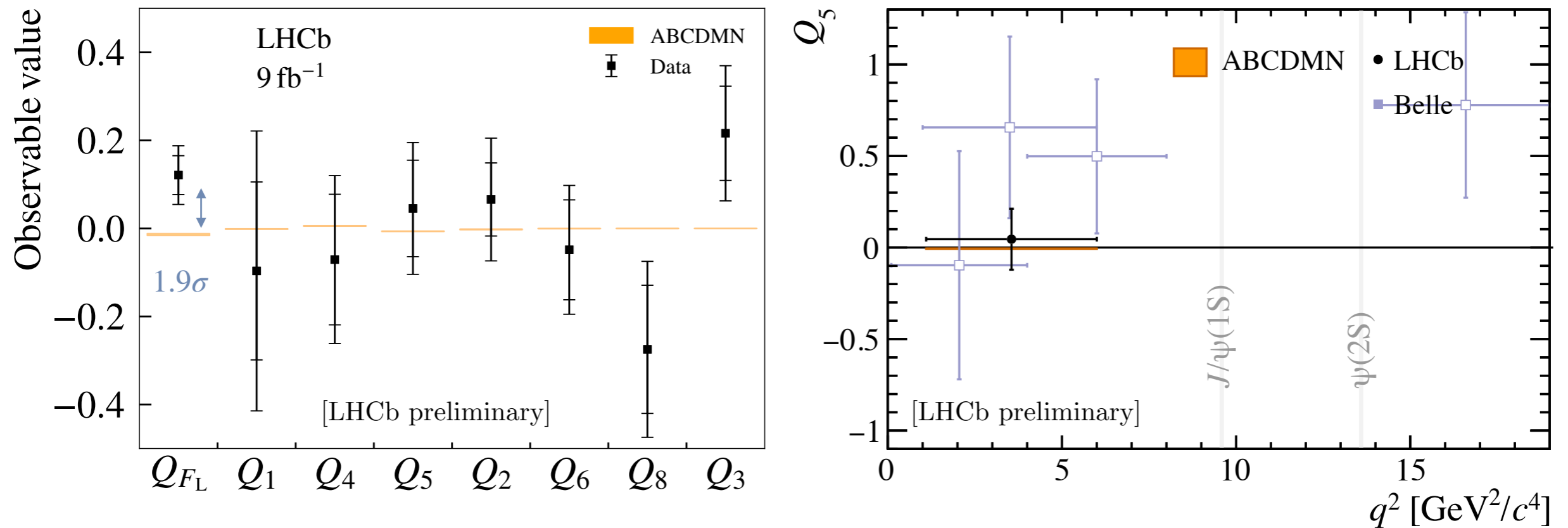
[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]

# LFU ANGULAR OBSERVABLES

LFU QUANTITIES ARE DERIVED BY COMPARING WITH MUON RESULTS [PRL 132 (2024) 131801]\*

$$Q_i = P_i^{(\mu)} - P_i^{(e)}$$



RESULTS ARE ALL CONSISTENT WITH THE LFU CONSERVATION HYPOTHESIS

[Belle Collaboration, PRL 118 (2017) 111801]

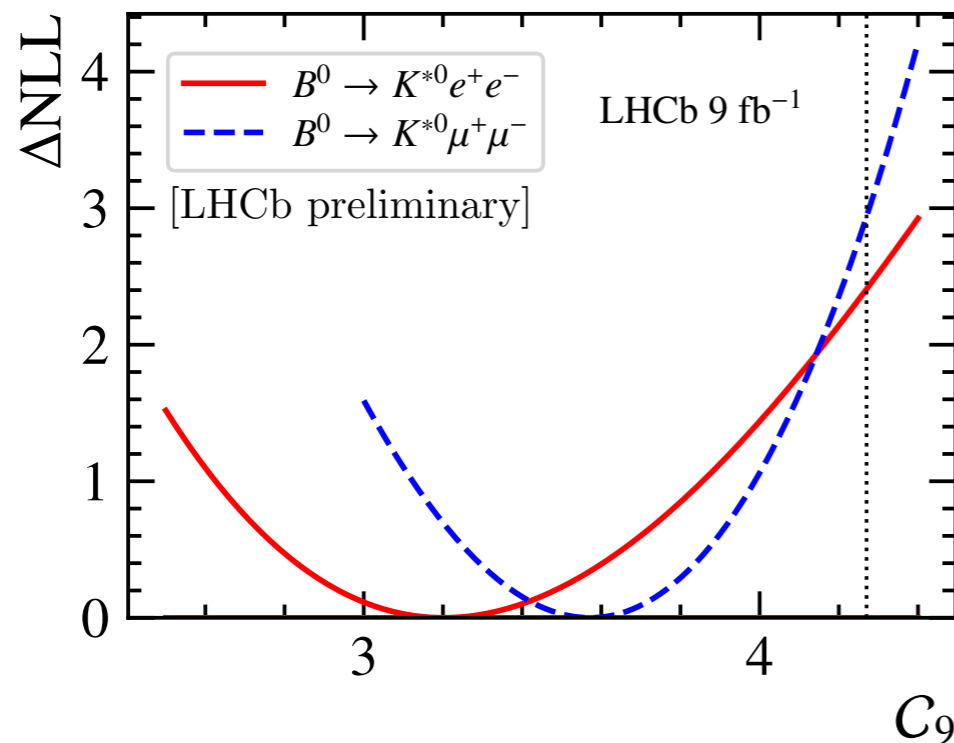
[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]

\*MUON DATA RE-ANALYSED WITHOUT EXPLICIT S-WAVE CONTRIBUTION

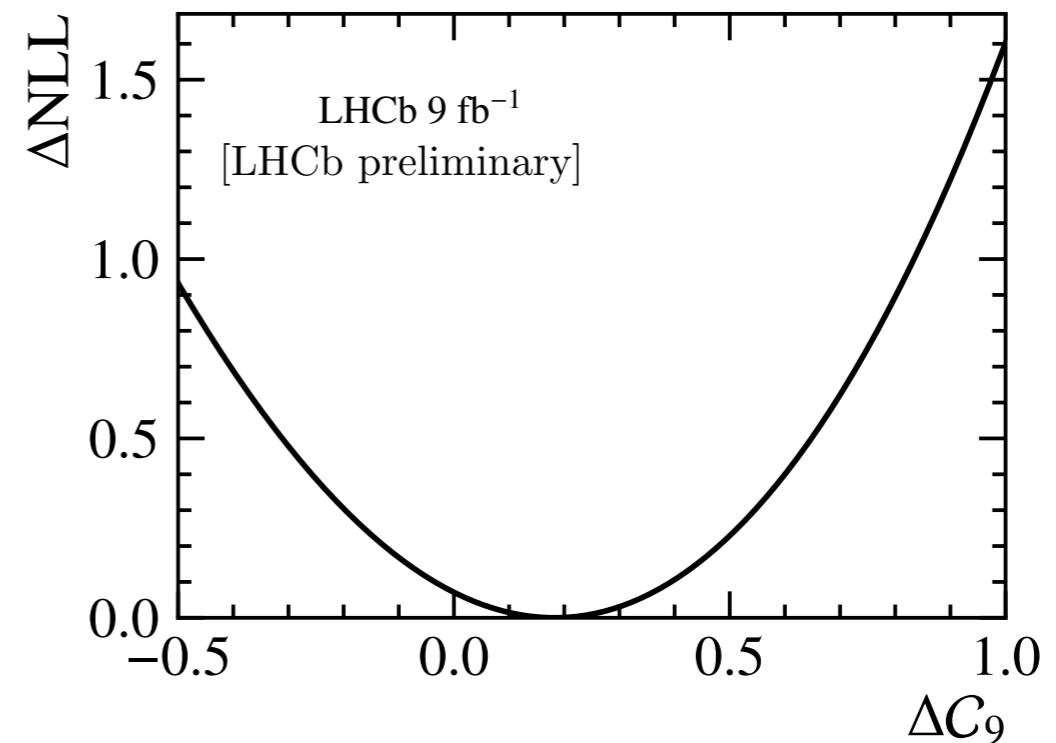
# WILSON COEFFICIENT INTERPRETATION

A GLOBAL FIT WITH ALL ANGULAR OBSERVABLES IS PERFORMED VARYING  $Re(C_9)$ :

- FORM FACTORS CONSTRAINED FROM [JHEP 12 (2023) 153] AND NON-LOCAL QCD TERMS FROM [JHEP 02 (2021) 088, JHEP 09 (2022) 133]
- LOCAL AND NON-LOCAL HADRONIC CONTRIBUTIONS ARE SHARED FOR THE TWO LEPTON SPECIES



SIMILAR PATTERN OF  
SHIFT IN  $Re(C_9)$



$$\Delta C_9 = C_9^{(\mu)} - C_9^{(e)} \text{ CONSISTENT WITH ZERO}$$

## SUMMARY

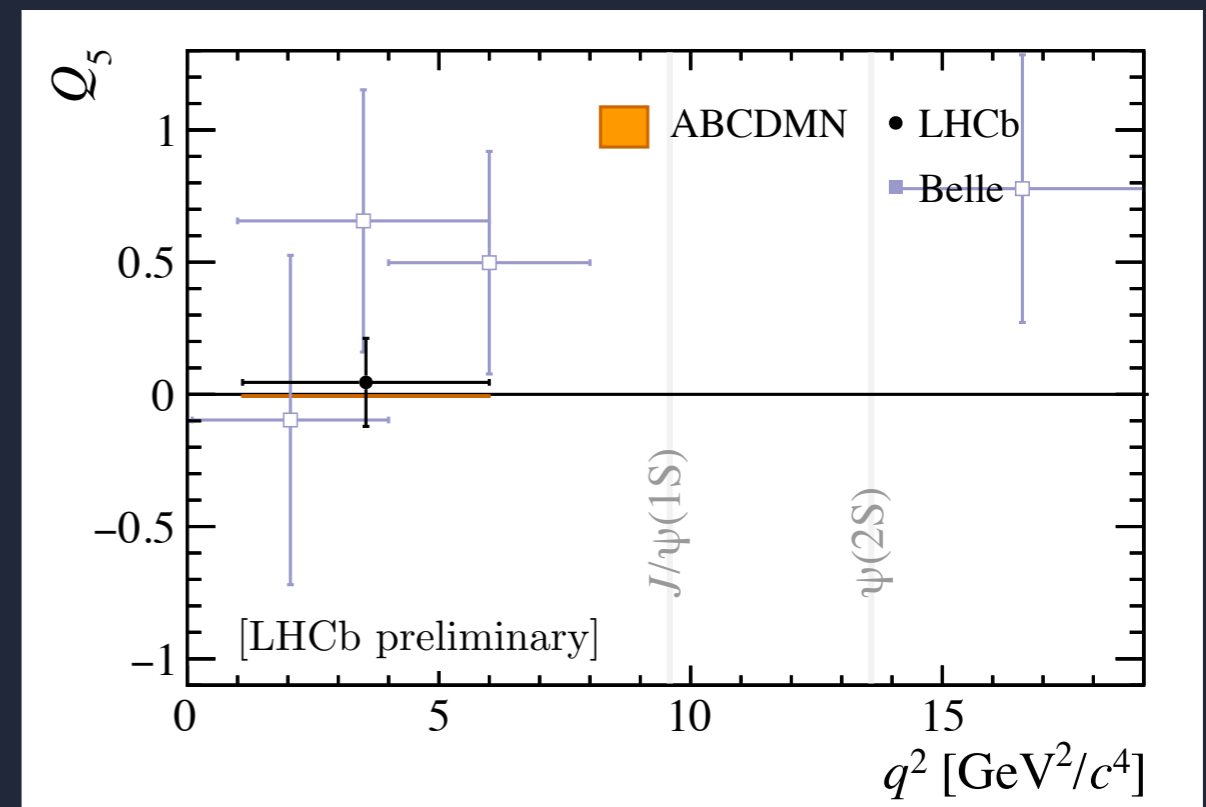
- FIRST ANGULAR ANALYSIS FOR ELECTRONS IN THE CENTRAL  $q^2$  REGION AT HADRONIC MACHINES

- BEST PRECISION OF ANGULAR OBSERVABLES

SENSITIVITY AT THE SAME LEVEL AS FIRST  $P'_5$  MEASUREMENT IN MUONS

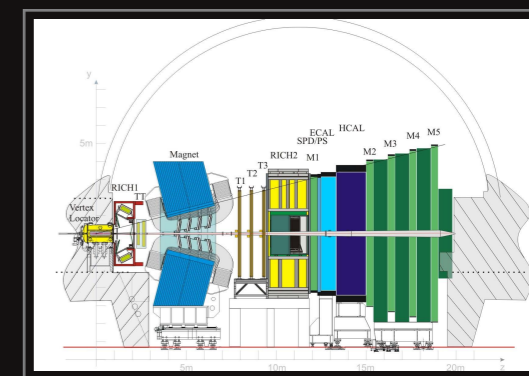
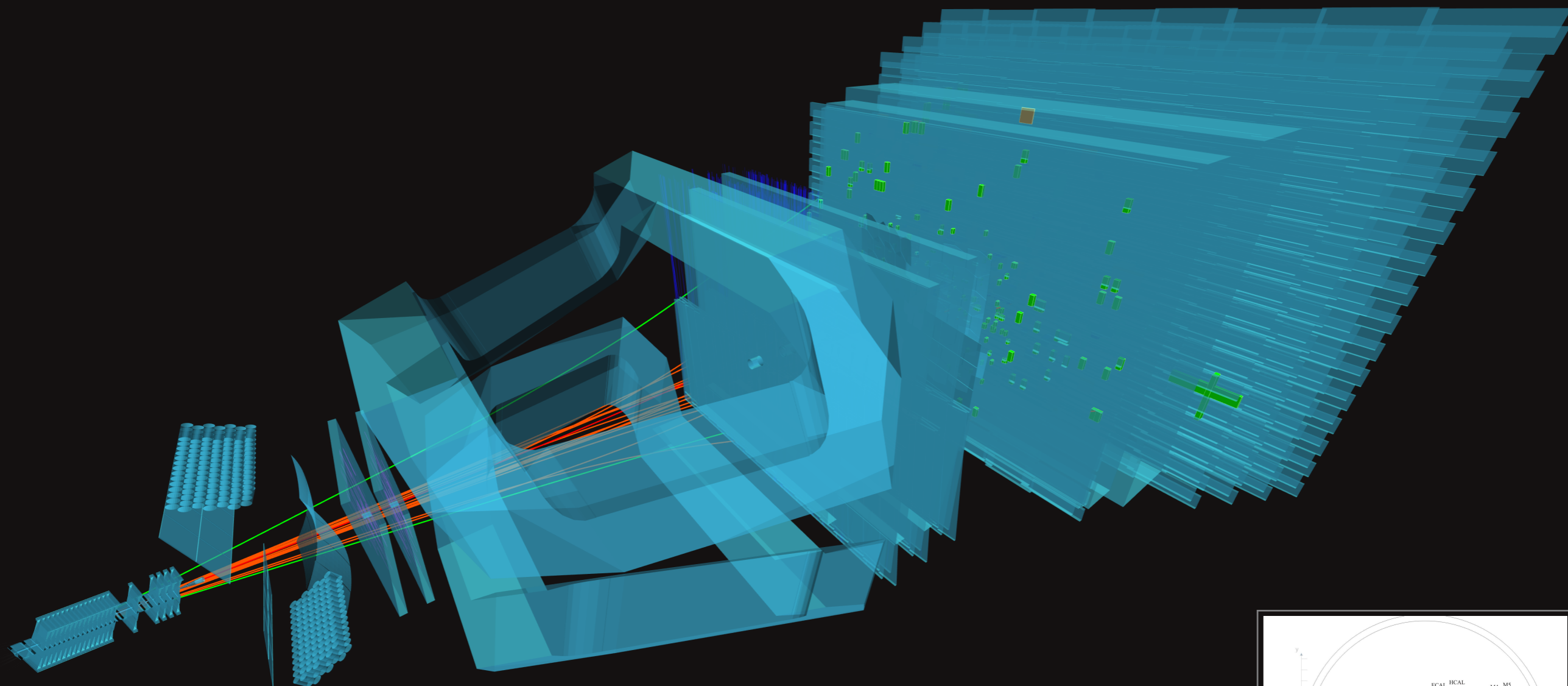


- RESULTS ARE CONSISTENT WITH THE SM AND WITH THE LFU HYPOTHESIS
- A GLOBAL FIT TO THE ANGULAR OBSERVABLES FAVOURS A SIMILAR PATTERN OF SHIFT IN  $Re(C_9)$  AS IN THE  $b \rightarrow s\mu^+\mu^-$  ANOMALIES
- MEASUREMENT OPENS EXPERIMENTAL VENUE FOR HIGH-PRECISION LFU/ANGULAR ANALYSIS WITH DATA FROM RUN 3 AND BEYOND



[Backup]

# The LHCb experiment

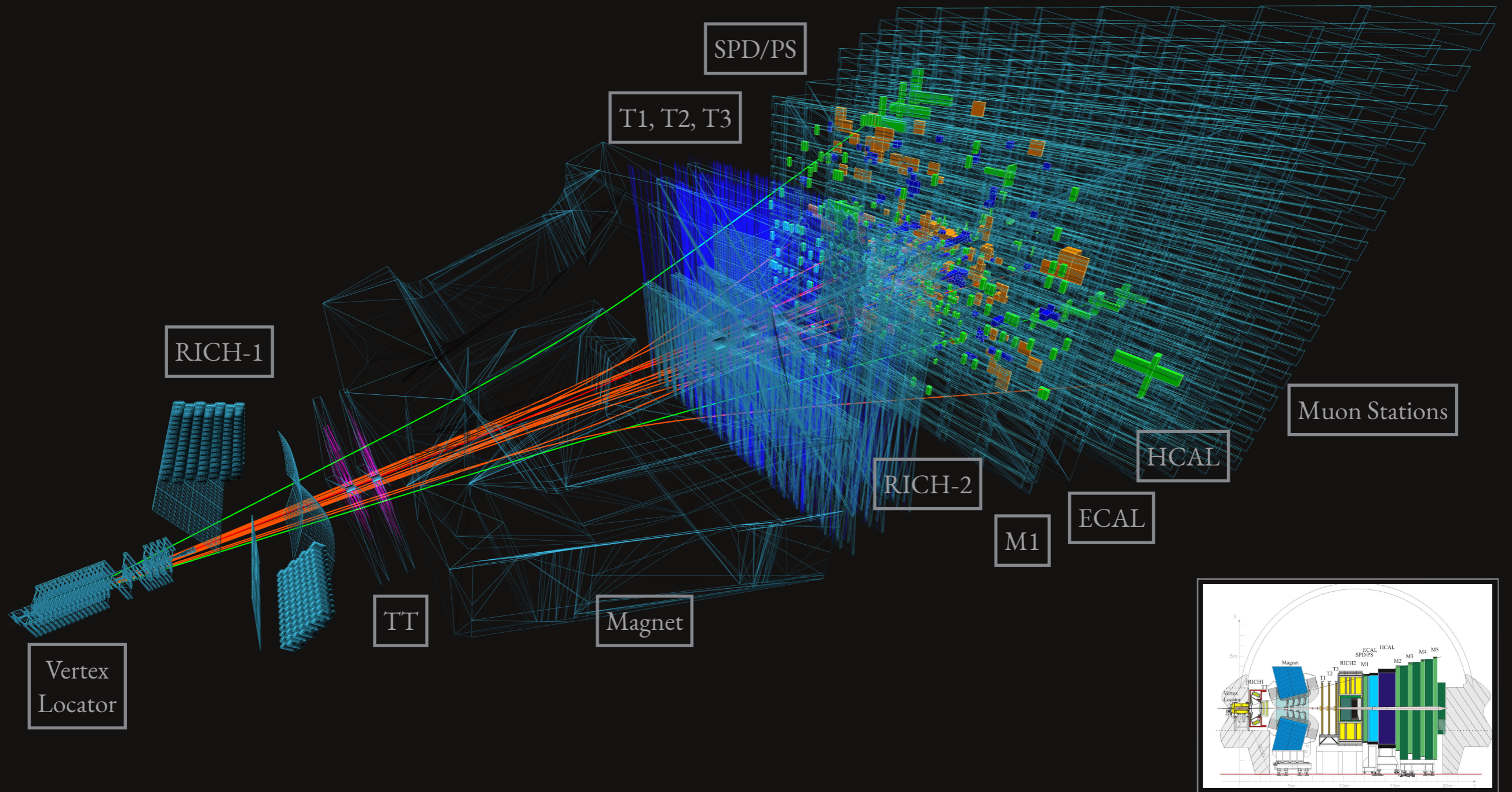


[Int. J. Mod. Phys. A30, (2015) 1530022]



[Backup]

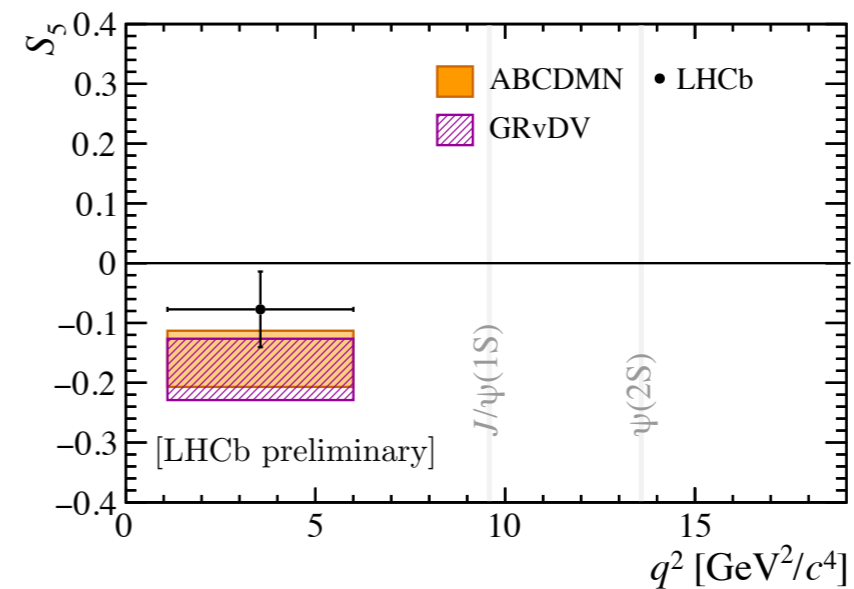
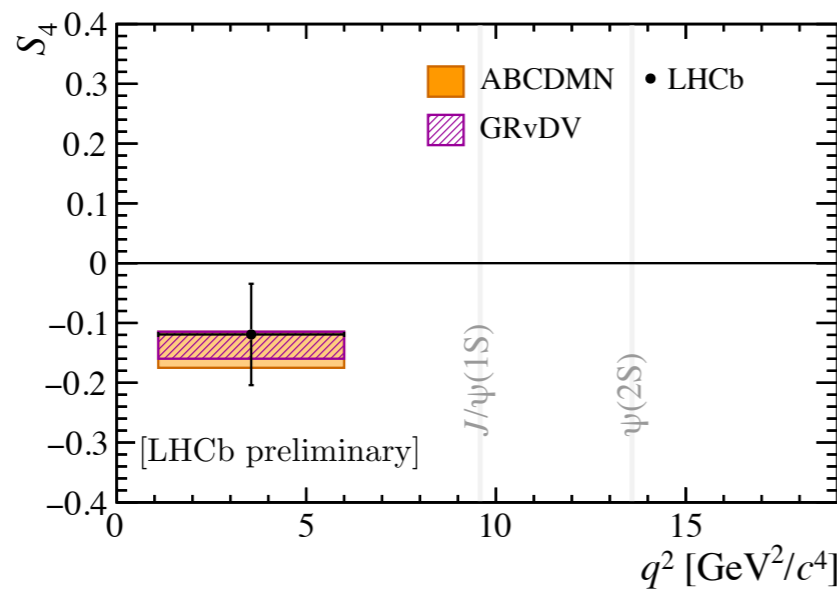
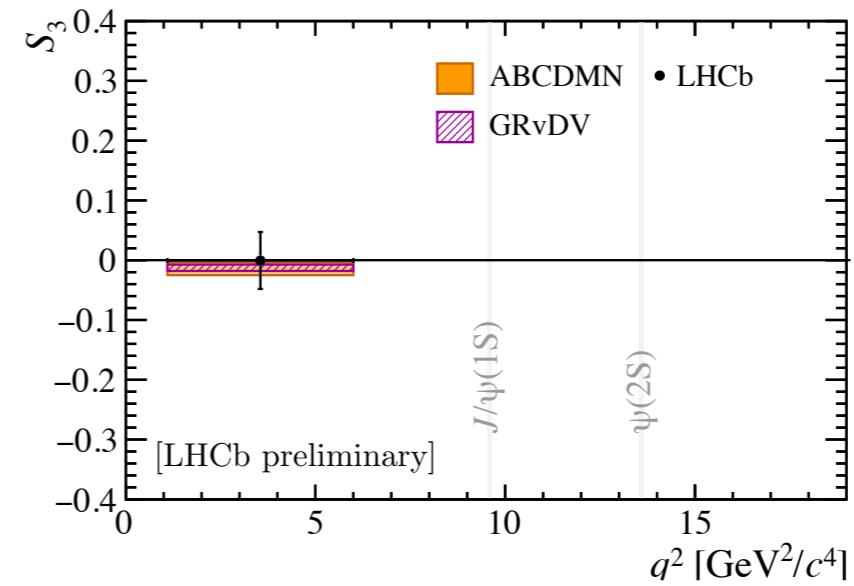
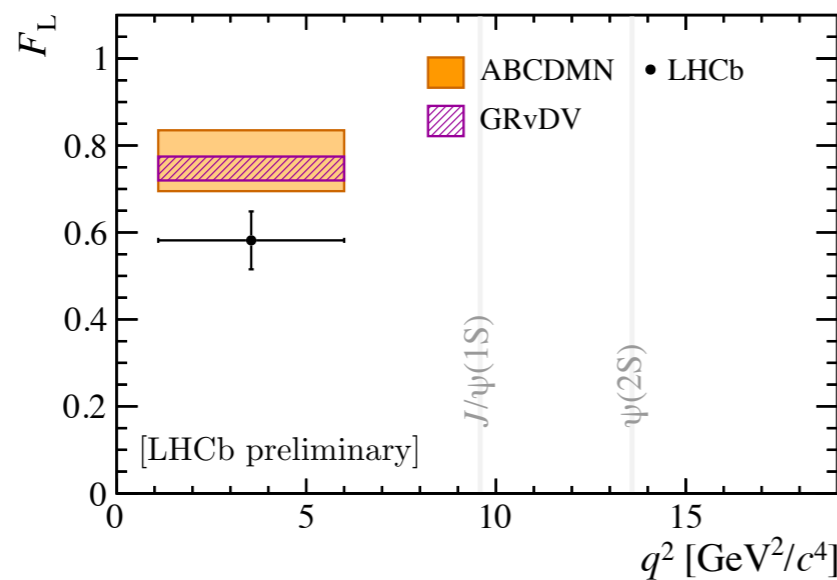
# The LHCb experiment



[Int. J. Mod. Phys. A30, (2015) 1530022]

# CP-AVERAGED ANGULAR OBSERVABLES

$S_i$  OBSERVABLES IN THE REGION BETWEEN [1.1, 6.0] GEV

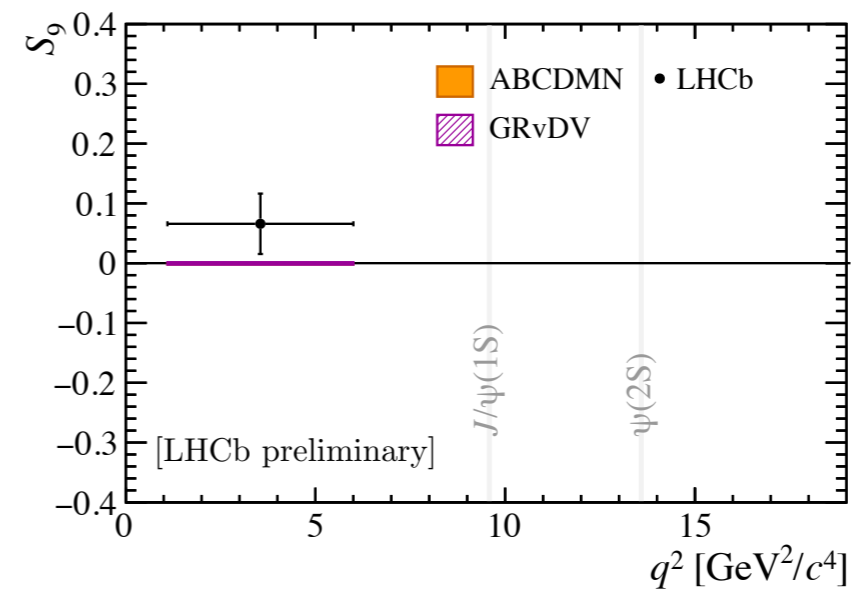
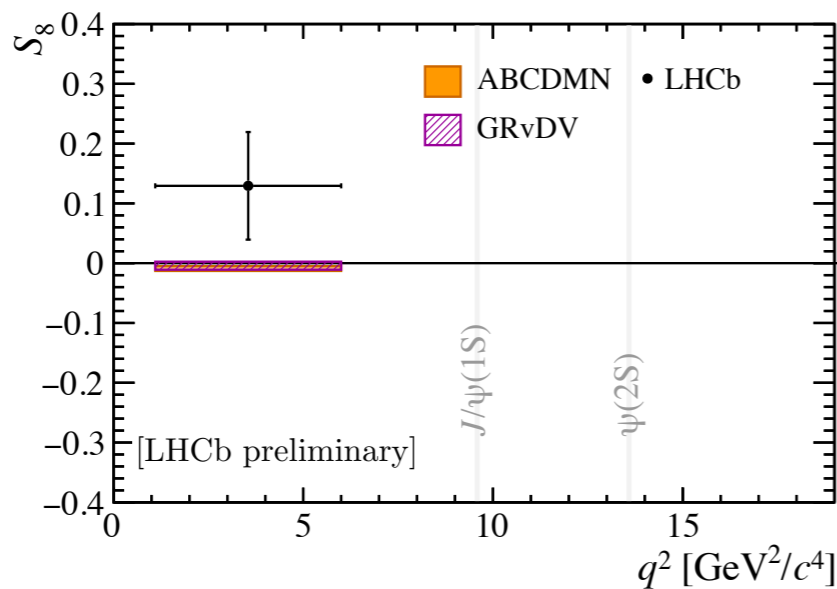
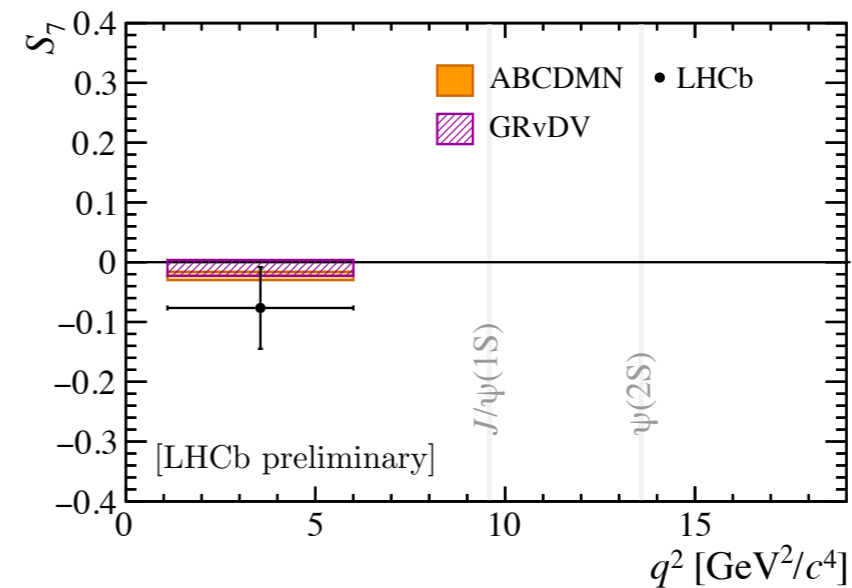
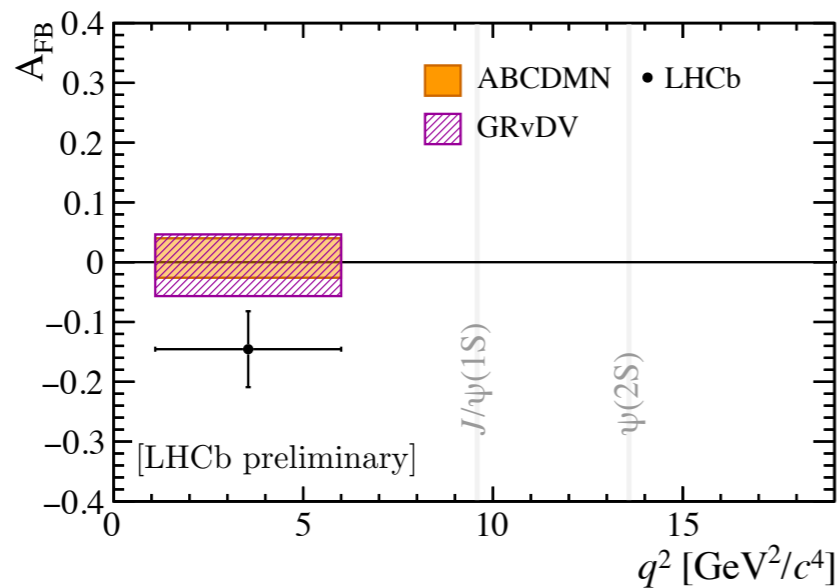


[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]

# CP-AVERAGED ANGULAR OBSERVABLES

$S_i$  OBSERVABLES IN THE REGION BETWEEN [1.1, 6.0] GEV

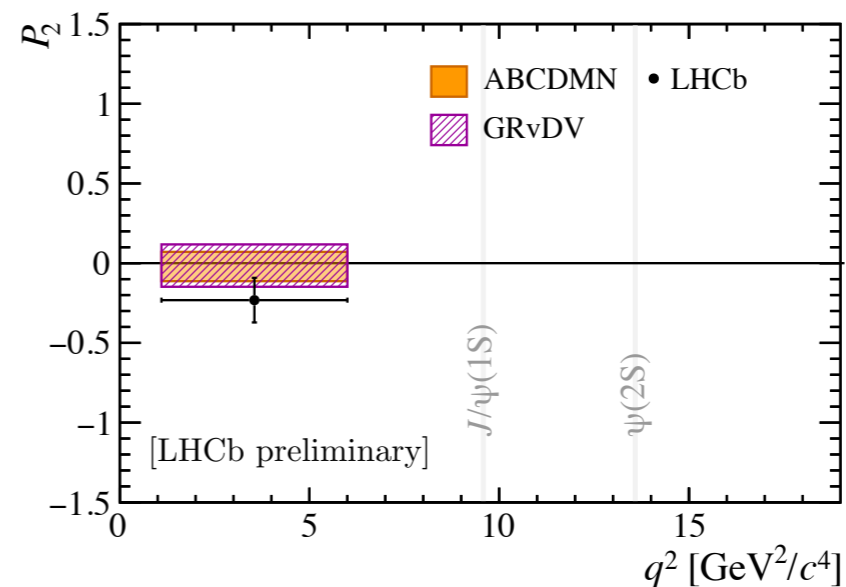
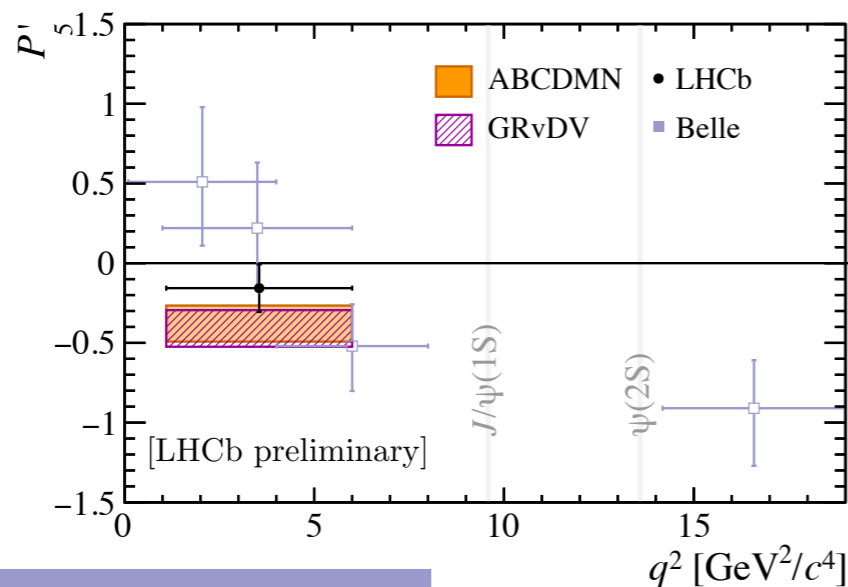
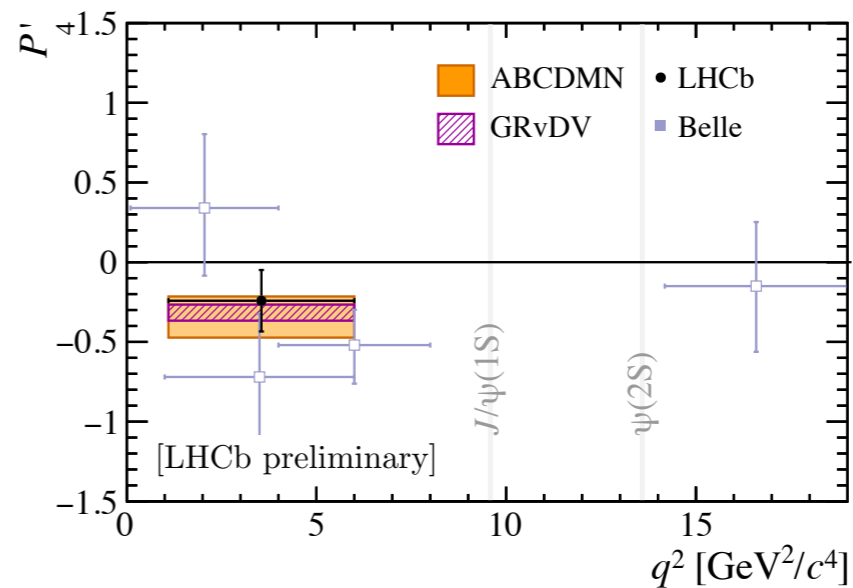
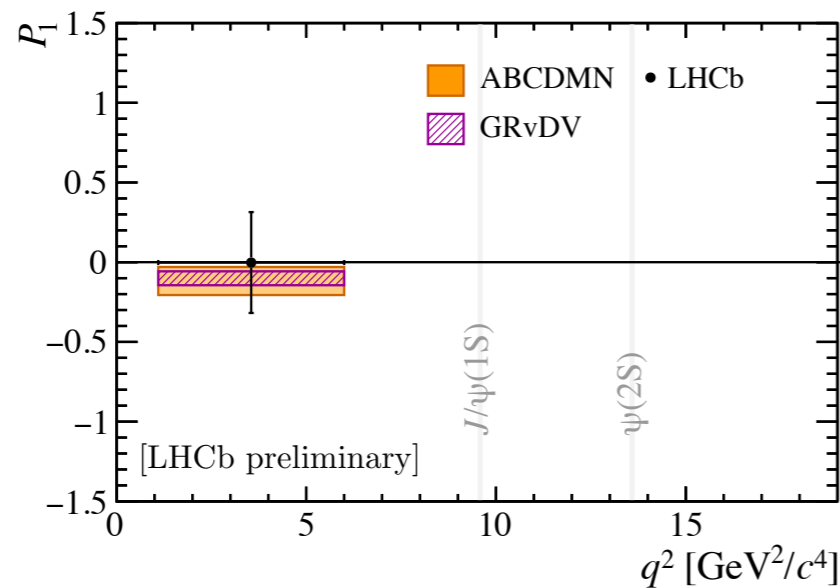


[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]

# CP-AVERAGED ANGULAR OBSERVABLES

$P_i^{(\cdot)}$  OBSERVABLES IN THE REGION BETWEEN [1.1, 6.0] GEV



[Belle Collaboration, PRL 118 (2017) 111801]

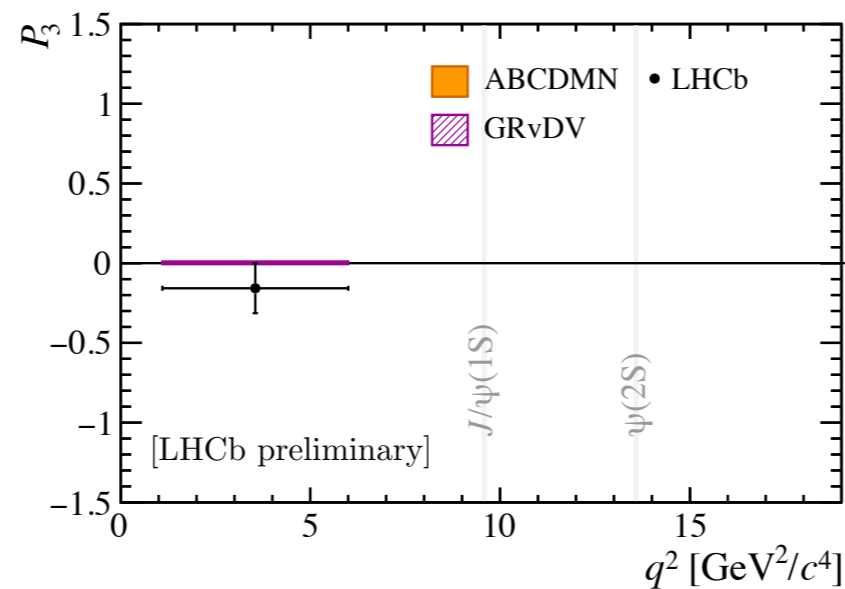
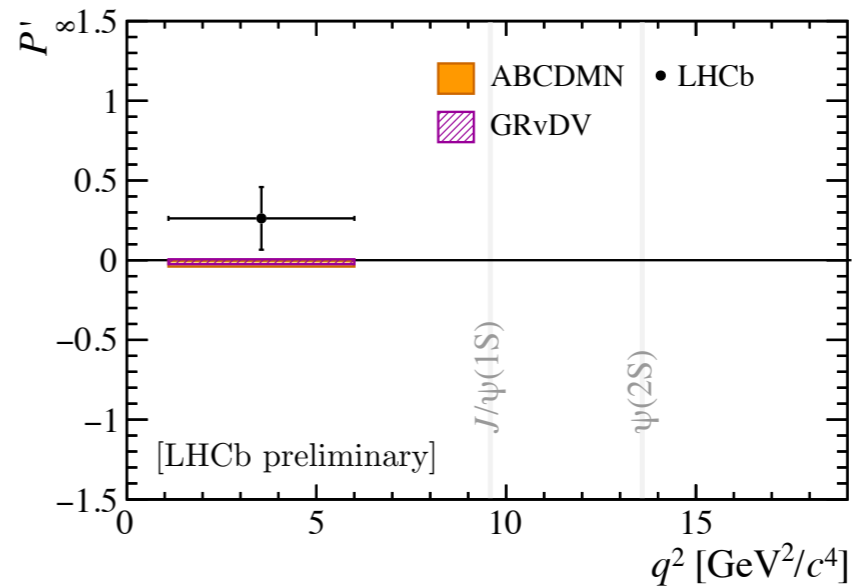
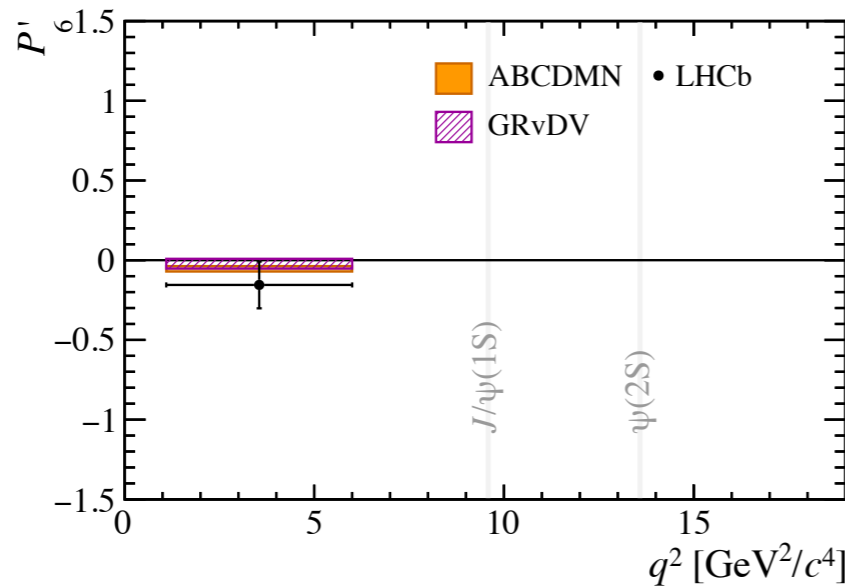
[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]



# CP-AVERAGED ANGULAR OBSERVABLES

$P_i^{(\cdot)}$  OBSERVABLES IN THE REGION BETWEEN [1.1, 6.0] GEV



[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]



# $S_i/P_i^{(\prime)}$ CORRELATION MATRIX

$S_i$  OBSERVABLES IN THE REGION BETWEEN [1.1, 6.0] GEV

[STATISTICAL]

	$F_L$	$S_3$	$S_4$	$S_5$	$A_{FB}$	$S_7$	$S_8$	$S_9$
$F_L$	1.00	0.01	-0.07	0.00	0.06	-0.01	-0.04	-0.06
$S_3$		1.00	-0.07	-0.02	0.05	0.10	-0.08	-0.01
$S_4$			1.00	-0.10	-0.10	-0.07	0.09	0.09
$S_5$				1.00	-0.05	0.06	-0.04	-0.03
$A_{FB}$					1.00	0.11	-0.07	-0.06
$S_7$						1.00	-0.07	-0.14
$S_8$							1.00	-0.01
$S_9$								1.00

[SYSTEMATICS]

	$F_L$	$S_3$	$S_4$	$S_5$	$A_{FB}$	$S_7$	$S_8$	$S_9$
$F_L$	1.000	0.008	-0.105	-0.151	-0.226	-0.015	0.014	-0.051
$S_3$		1.000	0.004	-0.055	0.002	0.007	0.015	0.014
$S_4$			1.000	0.354	0.013	-0.038	0.001	0.006
$S_5$				1.000	0.084	0.000	-0.033	0.007
$A_{FB}$					1.000	-0.017	-0.006	0.014
$S_7$						1.000	0.089	-0.044
$S_8$							1.000	-0.004
$S_9$								1.000

$P_i^{(\prime)}$  OBSERVABLES IN THE REGION BETWEEN [1.1, 6.0] GEV

[STATISTICAL]

	$F_L$	$P_1$	$P_2$	$P_3$	$P'_4$	$P'_5$	$P'_6$	$P'_8$
$F_L$	1.00	0.02	-0.20	-0.08	-0.09	-0.02	-0.02	-0.01
$P_1$		1.00	0.04	0.01	-0.07	-0.02	0.10	-0.08
$P_2$			1.00	0.06	-0.07	-0.05	0.11	-0.06
$P_3$				1.00	-0.08	0.03	0.14	0.02
$P'_4$					1.00	-0.10	-0.07	0.09
$P'_5$						1.00	0.06	-0.03
$P'_6$							1.00	-0.07
$P'_8$								1.00

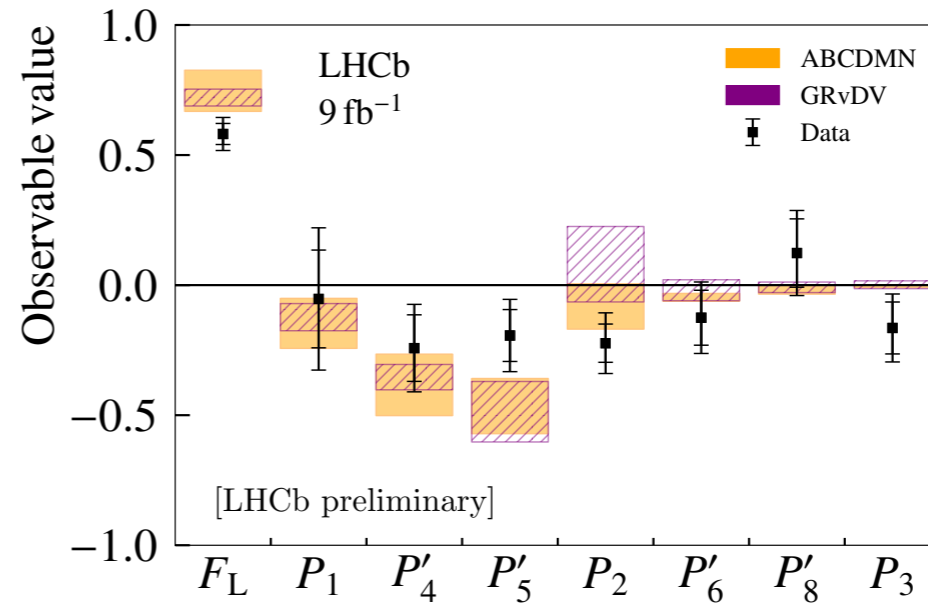
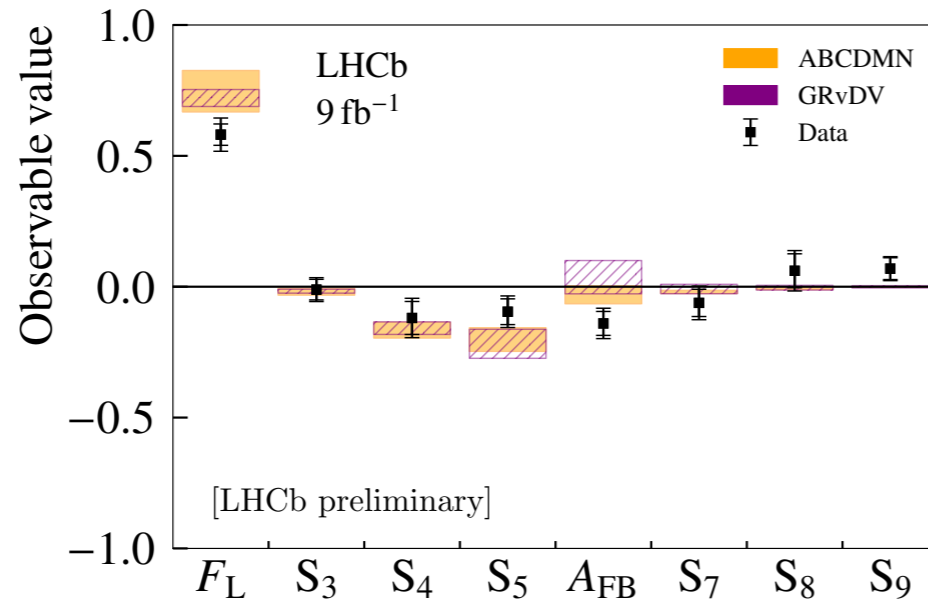
[SYSTEMATICS]

	$F_L$	$P_1$	$P_2$	$P_3$	$P'_4$	$P'_5$	$P'_6$	$P'_8$
$F_L$	1.00	-0.041	-0.142	0.023	-0.223	-0.326	-0.025	0.011
$P_1$		1.000	0.009	-0.012	0.001	-0.030	-0.009	0.009
$P_2$			1.000	0.017	0.067	0.127	0.016	-0.001
$P_3$				1.000	-0.004	0.002	0.042	0.004
$P'_4$					1.000	0.418	-0.010	0.000
$P'_5$						1.000	0.018	-0.025
$P'_6$							1.000	0.089
$P'_8$								1.000

# CP-AVERAGED ANGULAR OBSERVABLES

$$1.1 < q^2 < 7.0 \text{ GeV}^2/c^4$$

$F_L$	$0.581 \pm 0.041 \pm 0.049$		
$S_3$	$-0.011 \pm 0.039 \pm 0.023$	$P_1$	$-0.053 \pm 0.188 \pm 0.199$
$S_4$	$-0.119 \pm 0.063 \pm 0.041$	$P'_4$	$-0.242 \pm 0.128 \pm 0.109$
$S_5$	$-0.096 \pm 0.049 \pm 0.035$	$P'_5$	$-0.194 \pm 0.100 \pm 0.097$
$A_{\text{FB}}$	$-0.140 \pm 0.046 \pm 0.036$	$P_2$	$-0.223 \pm 0.074 \pm 0.090$
$S_7$	$-0.062 \pm 0.052 \pm 0.038$	$P'_6$	$-0.125 \pm 0.106 \pm 0.088$
$S_8$	$0.061 \pm 0.065 \pm 0.042$	$P'_8$	$0.123 \pm 0.131 \pm 0.098$
$S_9$	$0.069 \pm 0.042 \pm 0.019$	$P_3$	$-0.165 \pm 0.100 \pm 0.084$



[N. Gubernari, M. Reboud, D. Van Dyk, J. Virto, JHEP 09 (2022) 133]

[M. Algueró, A. Biswas, B. Capdevila, S. Descotes-Genon, J. Matias, EPJC 83 (2023) 7, 648]

# $S_i/P_i^{(\prime)}$ CORRELATION MATRIX

$S_i$  OBSERVABLES IN THE REGION BETWEEN [1.1, 7.0] GEV

[STATISTICAL]

	$F_L$	$S_3$	$S_4$	$S_5$	$A_{FB}$	$S_7$	$S_8$	$S_9$
$F_L$	1.0	0.02	-0.05	-0.01	0.09	-0.05	-0.03	-0.05
$S_3$		1.00	-0.05	-0.03	0.04	0.05	-0.05	0.02
$S_4$			1.00	-0.10	-0.14	-0.05	0.06	0.04
$S_5$				1.00	-0.07	0.06	-0.02	-0.04
$A_{FB}$					1.00	0.03	-0.04	-0.01
$S_7$						1.00	-0.06	-0.13
$S_8$							1.00	-0.04
$S_9$								1.00

[SYSTEMATICS]

	$F_L$	$S_3$	$S_4$	$S_5$	$A_{FB}$	$S_7$	$S_8$	$S_9$
$F_L$	1.000	0.010	-0.089	-0.134	-0.170	-0.016	0.015	-0.043
$S_3$		1.000	0.003	-0.049	-0.002	0.004	0.017	0.010
$S_4$			1.000	0.328	-0.008	-0.038	0.004	0.002
$S_5$				1.000	0.053	0.003	-0.04	-0.002
$A_{FB}$					1.000	-0.021	-0.006	0.011
$S_7$						1.000	0.114	-0.050
$S_8$							1.000	-0.006
$S_9$								1.000

$P_i^{(\prime)}$  OBSERVABLES IN THE REGION BETWEEN [1.1, 7.0] GEV

[STATISTICAL]

	$F_L$	$P_1$	$P_2$	$P_3$	$P'_4$	$P'_5$	$P'_6$	$P'_8$
$F_L$	1.00	0.00	-0.18	-0.11	-0.07	-0.04	-0.06	-0.02
$P_1$		1.00	0.04	-0.02	-0.05	-0.03	0.05	-0.05
$P_2$			1.00	0.03	-0.13	-0.06	0.05	-0.03
$P_3$				1.00	-0.03	0.04	0.14	0.04
$P'_4$					1.00	-0.10	-0.05	0.06
$P'_5$						1.00	0.06	-0.02
$P'_6$							1.00	-0.06
$P'_8$								1.00

[SYSTEMATICS]

	$F_L$	$P_1$	$P_2$	$P_3$	$P'_4$	$P'_5$	$P'_6$	$P'_8$
$F_L$	1.00	-0.037	-0.052	0.021	-0.185	-0.276	-0.023	0.009
$P_1$		1.00	0.004	-0.022	0.018	-0.014	0.005	0.016
$P_2$			1.00	0.009	-0.011	0.031	-0.008	0.000
$P_3$				1.000	-0.006	0.009	0.053	0.009
$P'_4$					1.000	0.368	-0.026	0.004
$P'_5$						1.000	0.011	-0.030
$P'_6$							1.000	0.113
$P'_8$								1.000

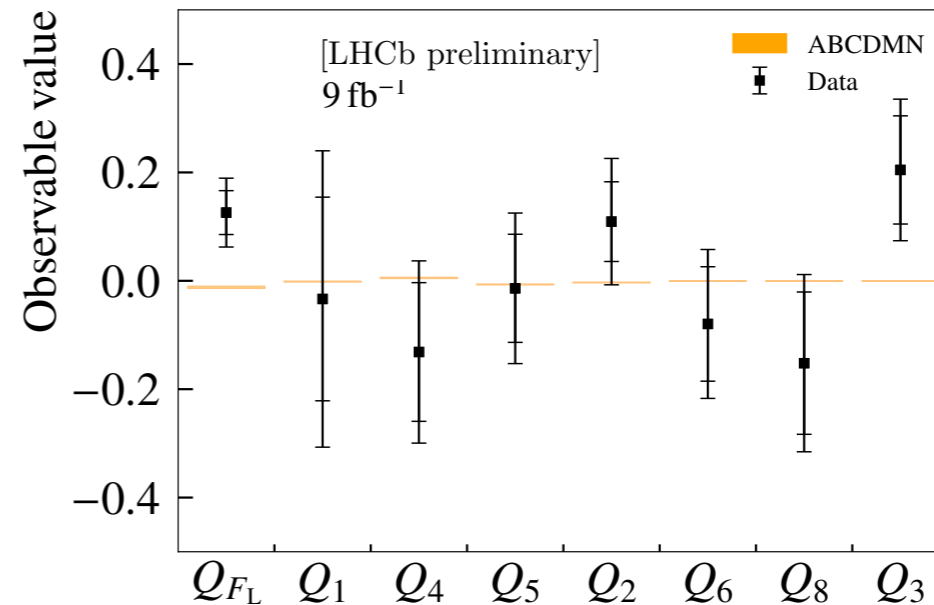
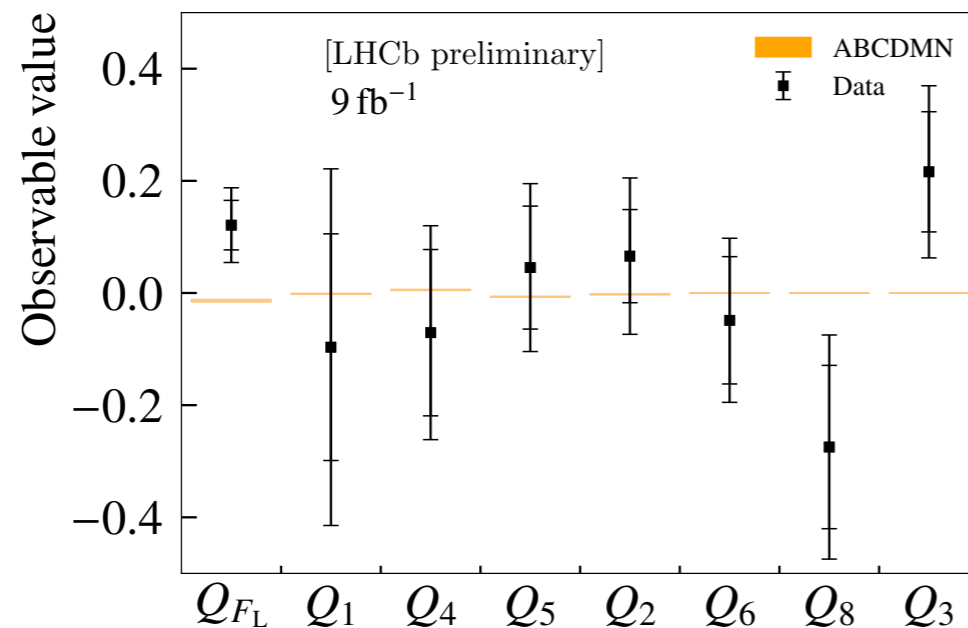
# LFU OBSERVABLES

$$1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$$

$Q_{FL}$	$0.121 \pm 0.050 \pm 0.050$
$Q_1$	$-0.097 \pm 0.264 \pm 0.246$
$Q_4$	$-0.071 \pm 0.173 \pm 0.120$
$Q_5$	$0.045 \pm 0.132 \pm 0.102$
$Q_2$	$0.066 \pm 0.098 \pm 0.112$
$Q_6$	$-0.049 \pm 0.137 \pm 0.092$
$Q_8$	$-0.275 \pm 0.166 \pm 0.137$
$Q_3$	$0.216 \pm 0.144 \pm 0.110$

$$1.1 < q^2 < 7.0 \text{ GeV}^2/c^4$$

$Q_{FL}$	$0.126 \pm 0.046 \pm 0.049$
$Q_1$	$-0.034 \pm 0.246 \pm 0.199$
$Q_4$	$-0.131 \pm 0.149 \pm 0.109$
$Q_5$	$-0.014 \pm 0.119 \pm 0.097$
$Q_2$	$0.109 \pm 0.086 \pm 0.091$
$Q_6$	$-0.080 \pm 0.124 \pm 0.088$
$Q_8$	$-0.152 \pm 0.149 \pm 0.098$
$Q_3$	$0.205 \pm 0.131 \pm 0.084$



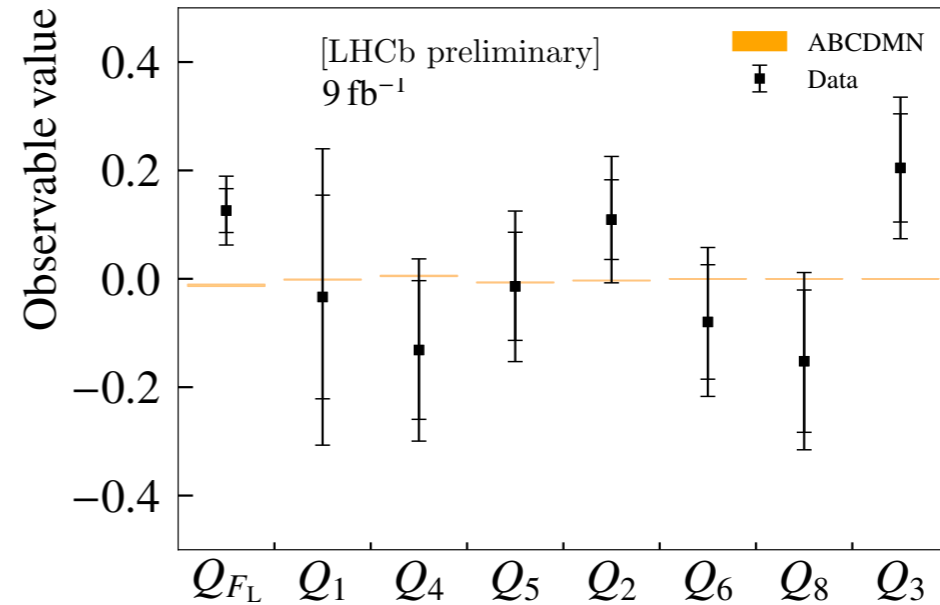
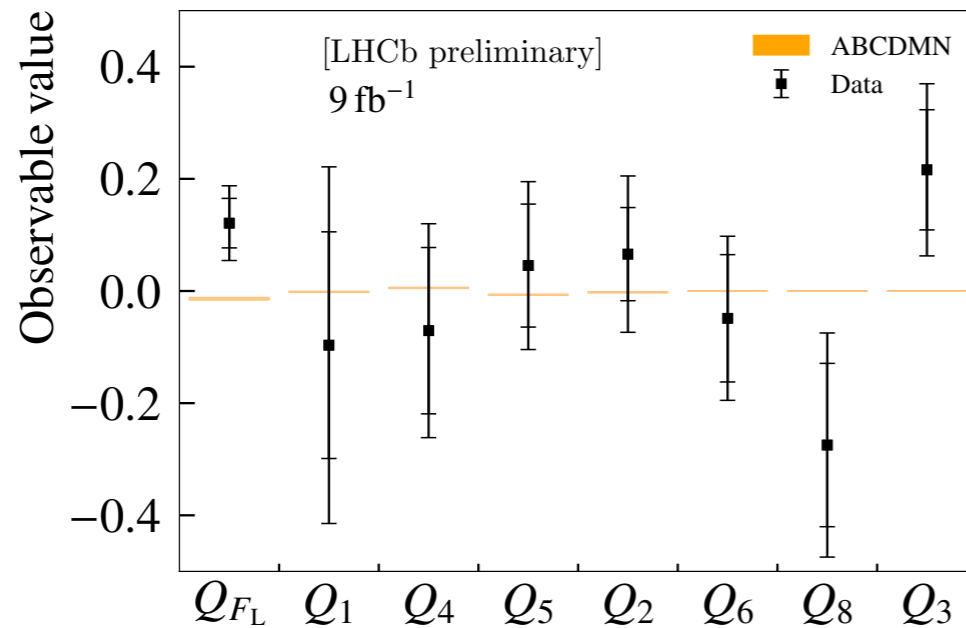
# LFU OBSERVABLES

$$1.1 < q^2 < 6.0 \text{ GeV}^2/c^4$$

$Q_{FL}$	$0.121 \pm 0.050 \pm 0.050$
$Q_1$	$-0.097 \pm 0.264 \pm 0.246$
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$$1.1 < q^2 < 7.0 \text{ GeV}^2/c^4$$

$Q_{FL}$	$0.126 \pm 0.046 \pm 0.049$
$Q_1$	$-0.034 \pm 0.246 \pm 0.199$
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$Q_3$	$0.205 \pm 0.131 \pm 0.084$

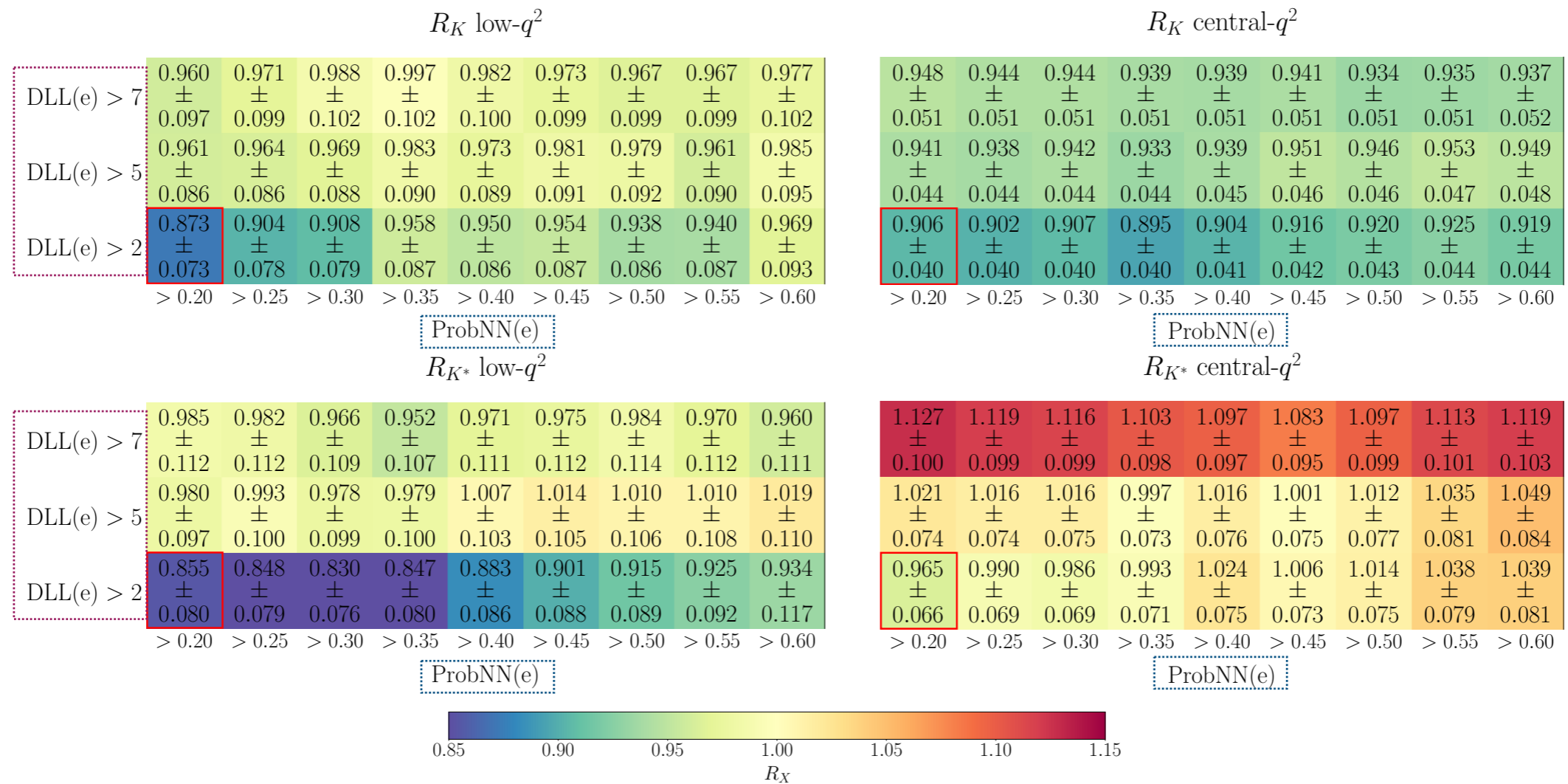


# MISIDENTIFIED BACKGROUND PROCEDURE

[PRL 131 (2023) 051803, PRD 108 (2023) 032002]

## TIGHTENING ELECTRON PID EXHIBITS A COHERENT PATTERN

INVERT PID REQUIREMENTS ON ONE OR BOTH ELECTRONS (CONTROL CHANNEL)



DLL(E): COMBINATION OF SUB-DETECTORS DELTA LOG-LIKEHOOD FOR  $\pi, e$

PROBNN(E): NEURAL-NET BASED E-ID SCORE

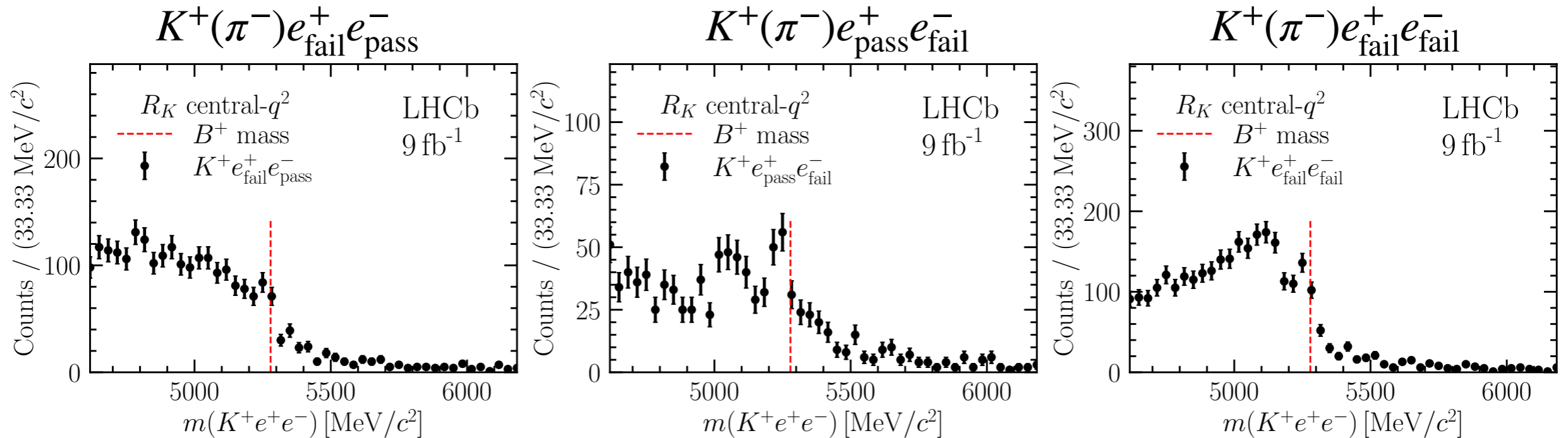


# MISIDENTIFIED BACKGROUND PROCEDURE

EXAMPLE FROM [PRL 131 (2023) 051803, PRD 108 (2023) 032002]

INVERT PID REQUIREMENTS ON ONE OR BOTH ELECTRONS (CONTROL CHANNEL)

## CONTROL REGIONS

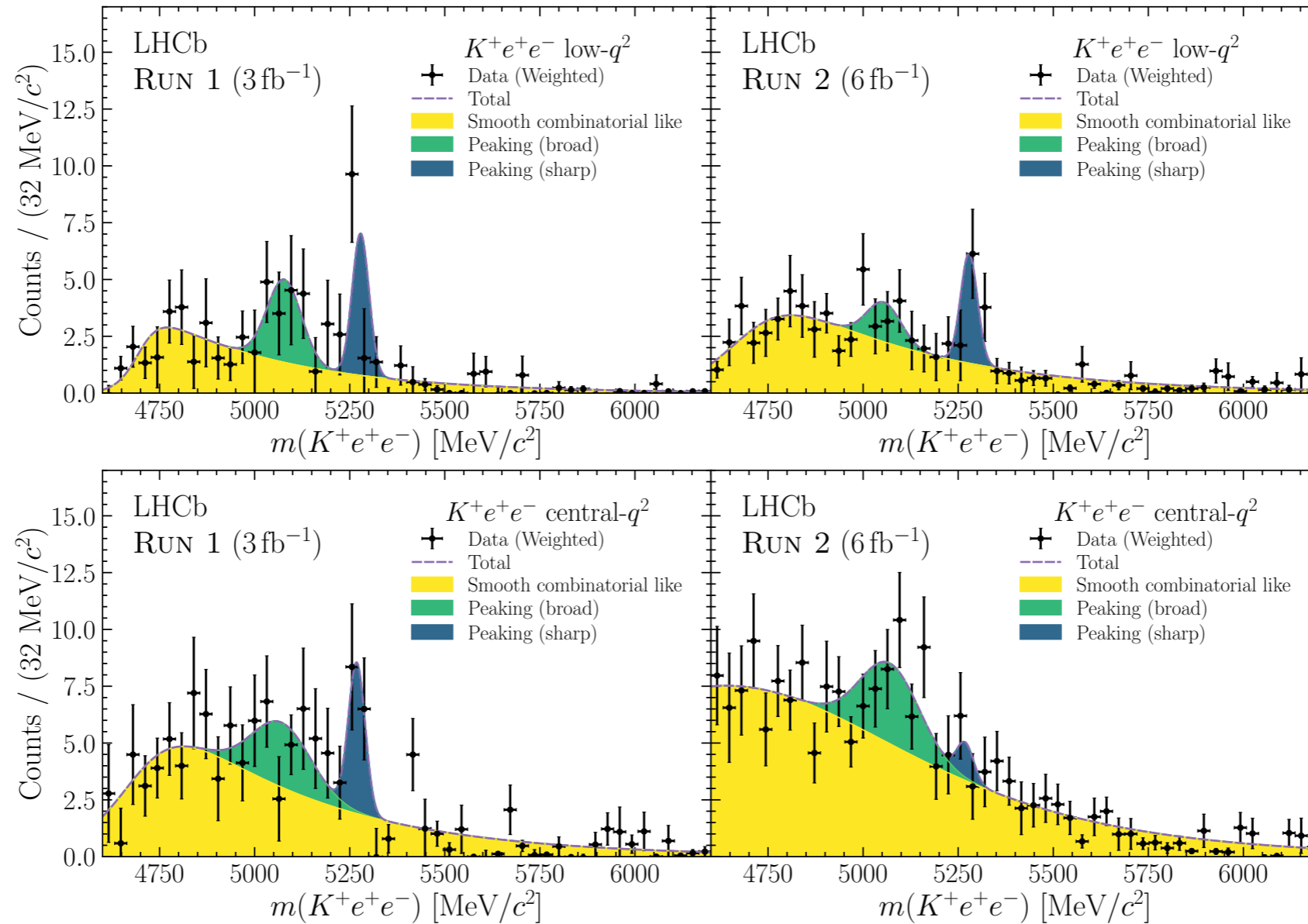


CATEGORISE PION- AND KAON-LIKE ELECTRONS IN CONTROL REGION WITH NEURAL-NET ID

PARAMETRISE SHAPE AND PREDICT NORMALISATION OF SUCH CONTRIBUTION

# MISIDENTIFIED BACKGROUND PROCEDURE

EXAMPLE FROM [PRL 131 (2023) 051803, PRD 108 (2023) 032002]



SIMILAR MISIDENTIFIED BACKGROUND MODELLING FOR  $R_{K^*}$

# MISIDENTIFIED BACKGROUND PROCEDURE

EXAMPLE FROM [PRL 131 (2023) 051803, PRD 108 (2023) 032002]

